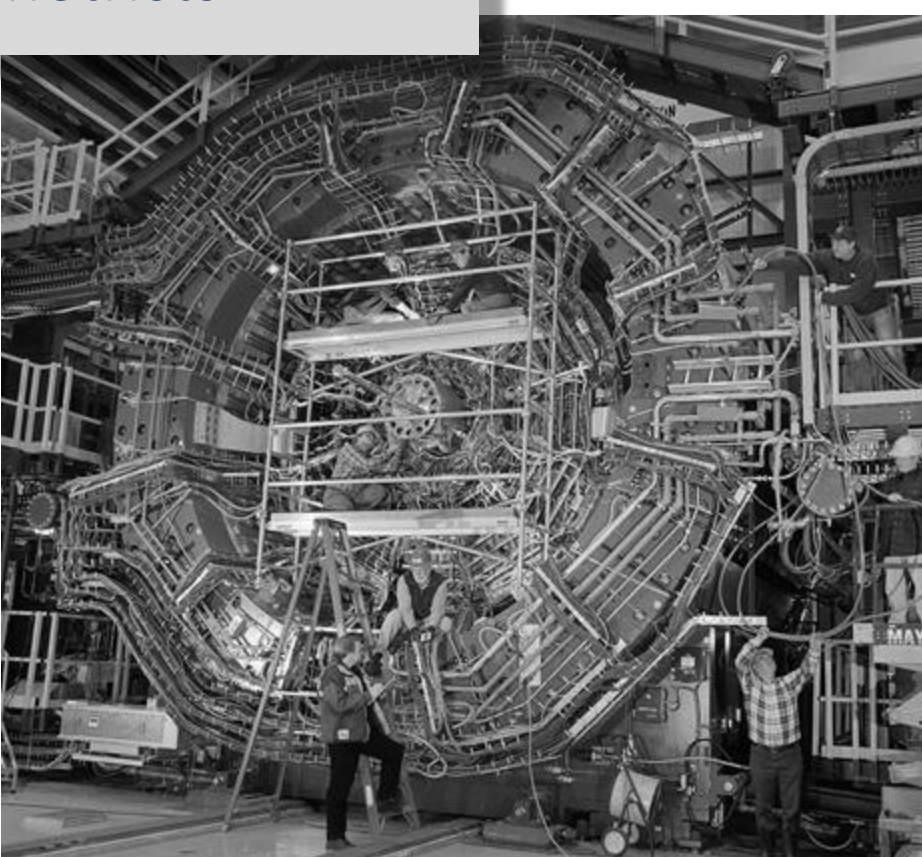
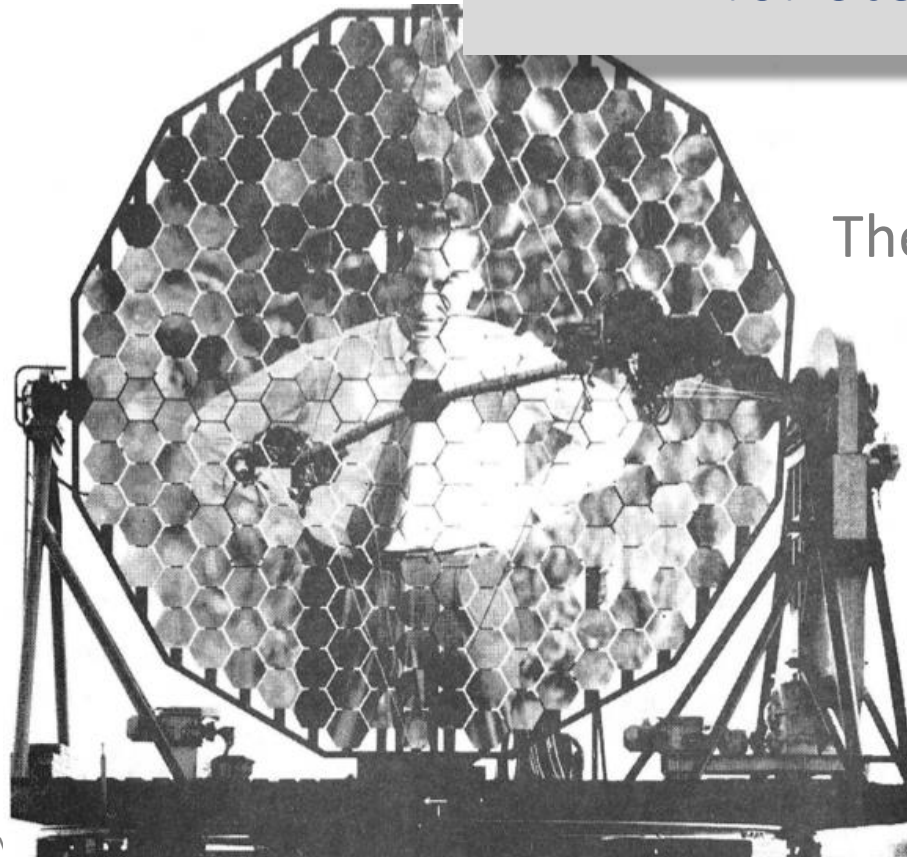
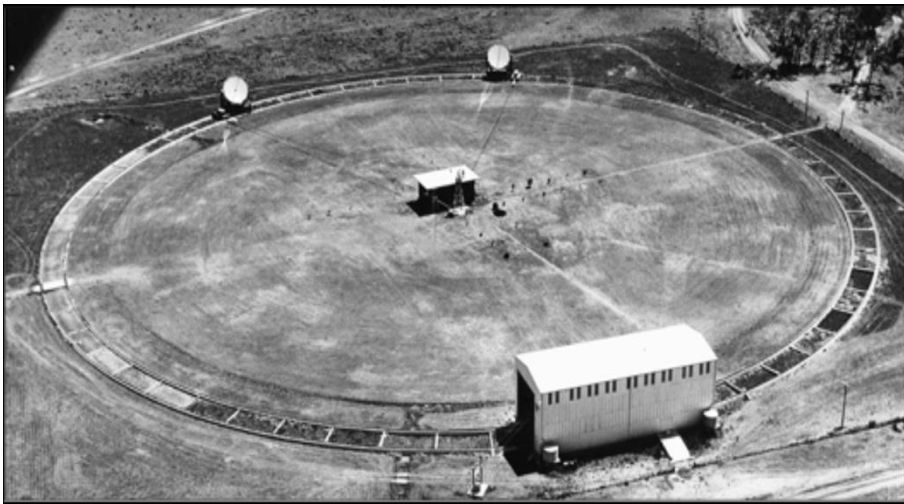


Subatomic Intensity Interferometry 101 for Stellar Intensity Interferometrists

Mike Lisa

The Ohio State University



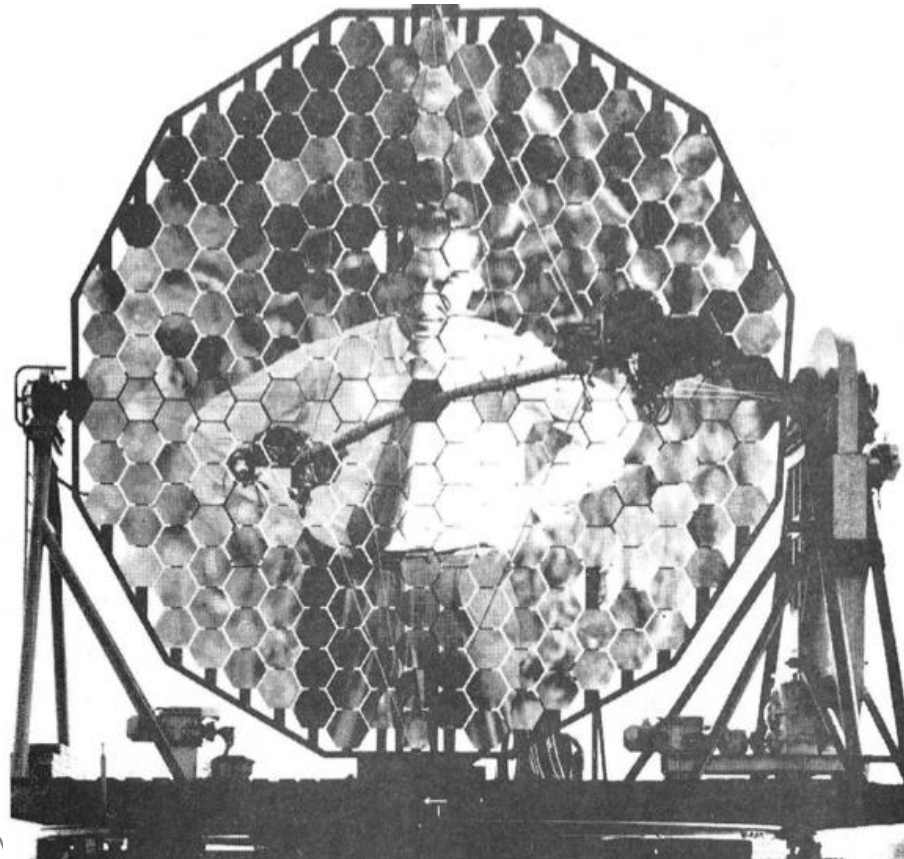


ring diameter

- Narrabri: 188 m
- RHIC* 1200 m

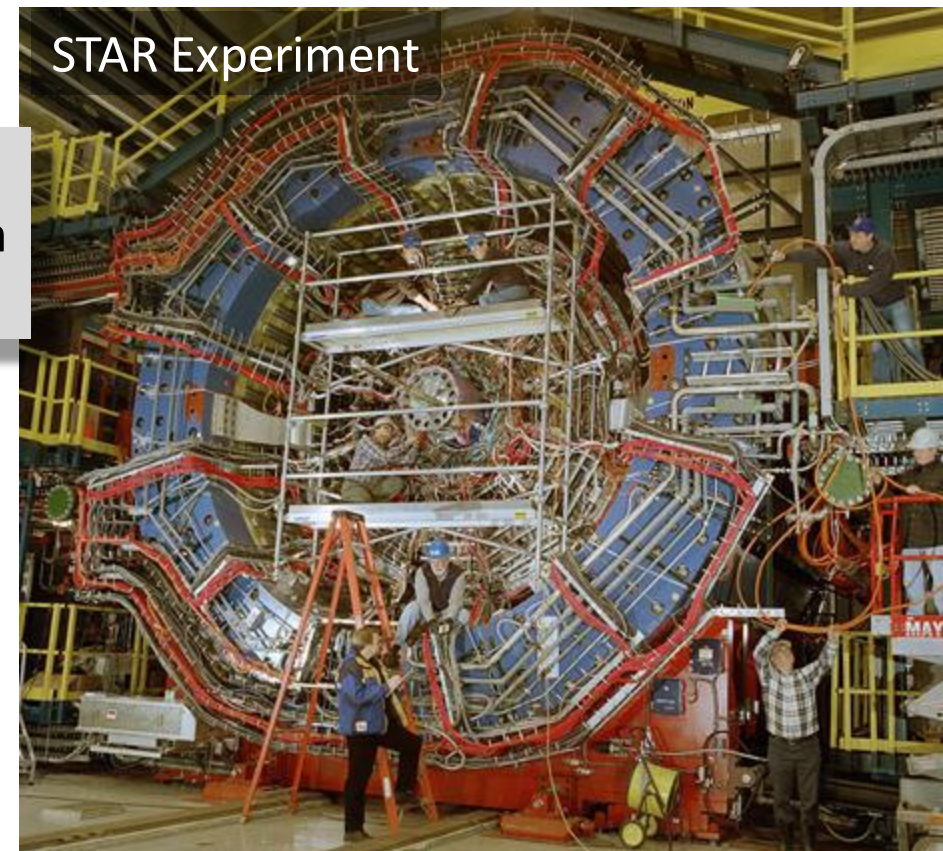


Relativistic Heavy Ion Collider



dodecagon detectors

- Narrabri mirrors: 6.5 m
- STAR detector: 6 m

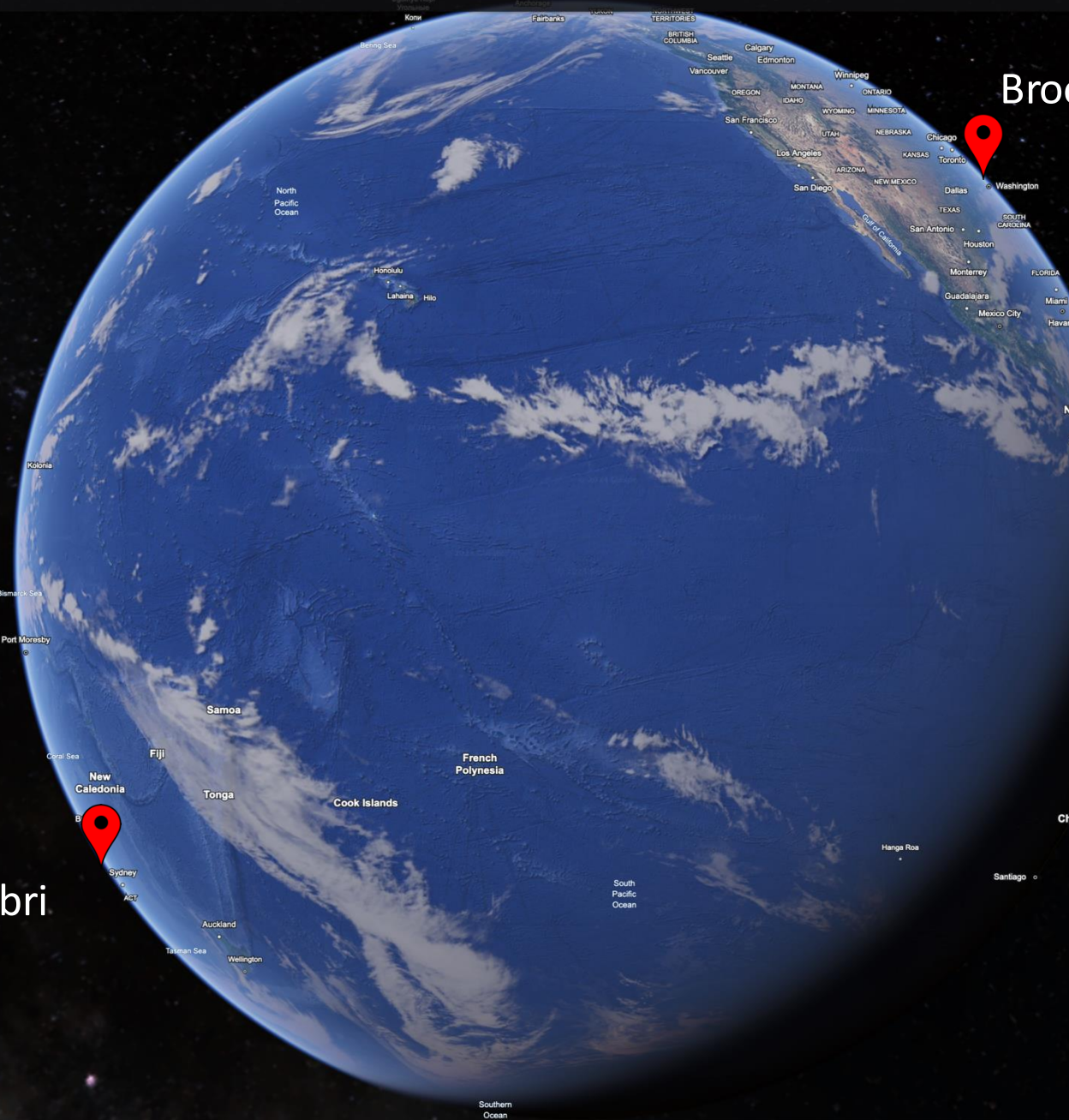


STAR Experiment

A world apart?

Brookhaven Lab, NY

Narrabri



CRIS '98 – Workshop on subatomic intensity interferometry. Catania Italy

your speaker

Robert Hanbury Brown



Hanbury Brown's one-sentence abstract:

The talk will give a brief history of the early development of Intensity Interferometry and its subsequent battle against common sense.



Robert Hanbury Brown

Outline

- Discovery of the “GGLP effect” & connection to HBT
- Relativistic heavy ion physics: motivation & importance of spacetime info
- Subatomic intensity interferometry (femtoscscopy)
- Summary

- Hanbury Brown & Twiss – 1954
- 1955 – discovery of antiproton
- 1960 – GGLP

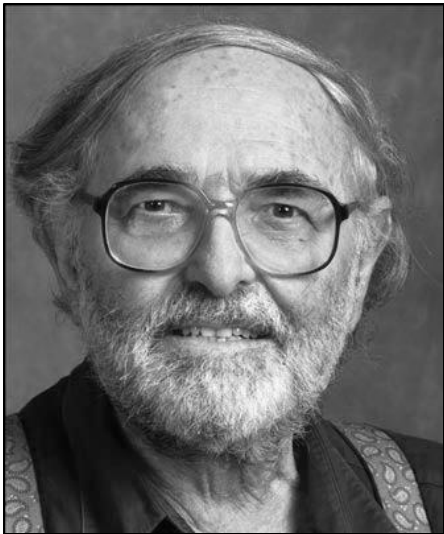
PHYSICAL REVIEW

VOLUME 120, NUMBER 1

OCTOBER 1, 1960

Influence of Bose-Einstein Statistics on the Antiproton-Proton Annihilation Process*

GERSON GOLDHABER, SULAMITH GOLDHABER, WONYONG LEE, AND ABRAHAM PAIS†
Lawrence Radiation Laboratory and Department of Physics, University of California, Berkeley, California
(Received May 16, 1960)



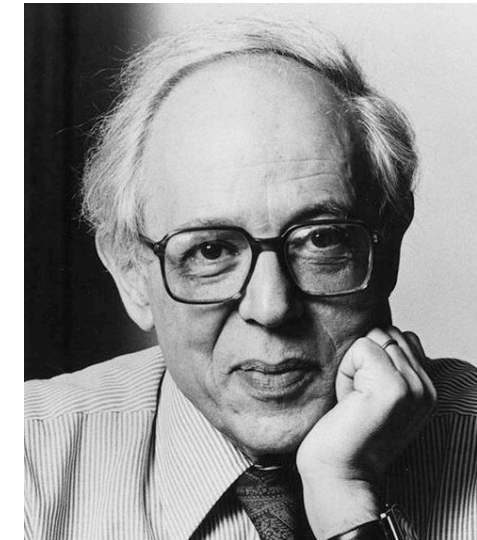
Gershon Goldhaber



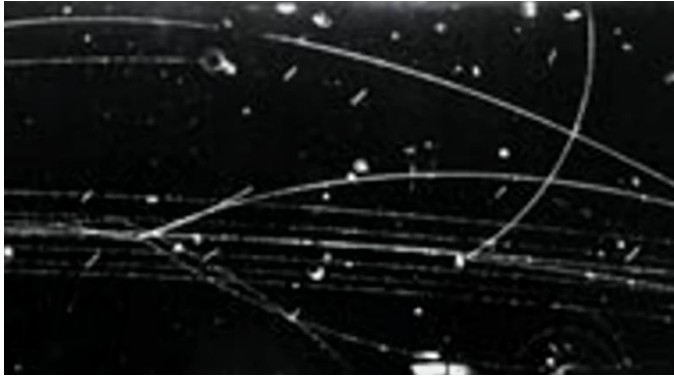
Sulamith Goldhaber



Wonyong Lee



Abraham Pais

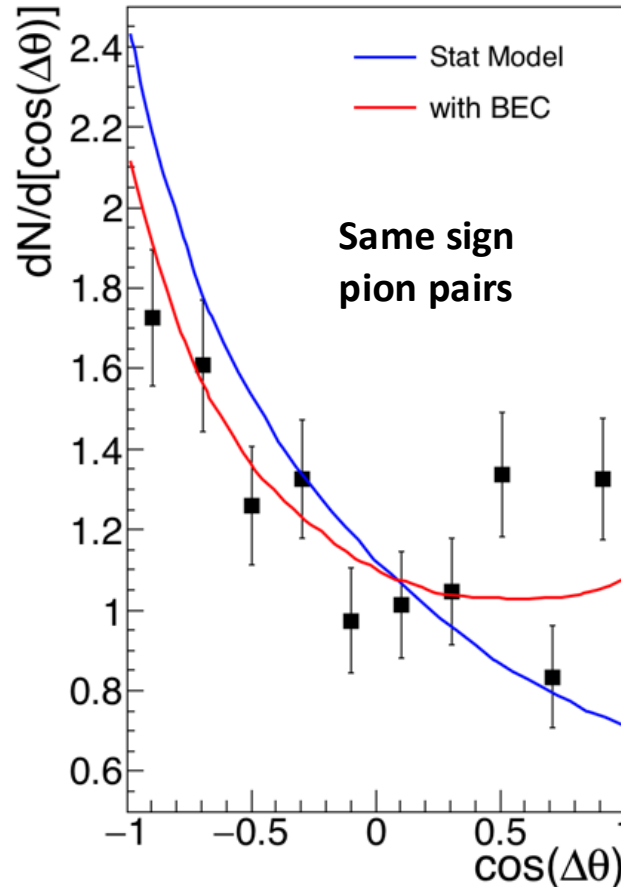


Influence of Bose-Einstein Statistics on the Antiproton-Proton Annihilation Process*

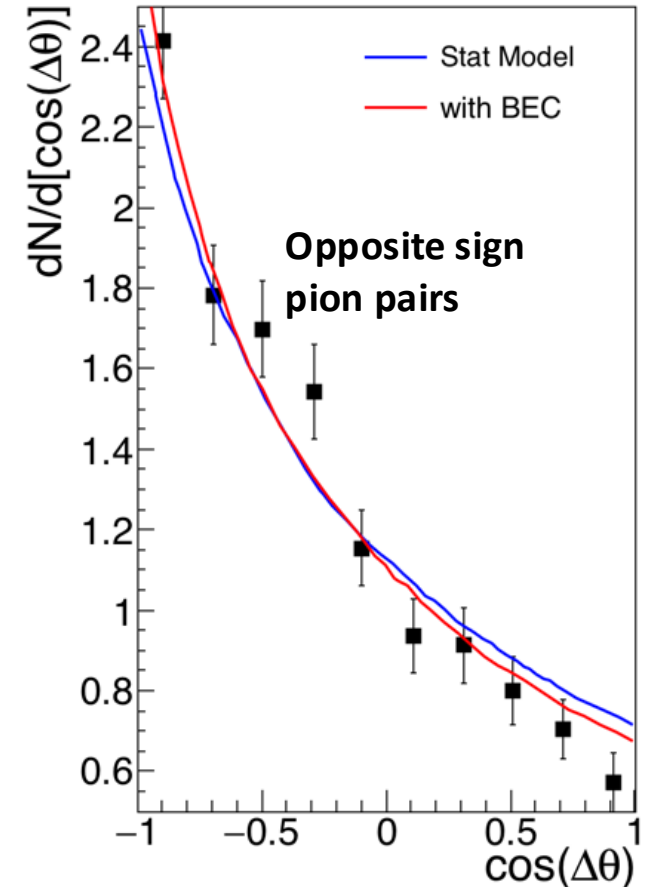
GERSON GOLDHABER, SULAMITH GOLDHABER, WONYONG LEE, AND ABRAHAM PAIS†
Lawrence Radiation Laboratory and Department of Physics, University of California, Berkeley, California
(Received May 16, 1960)

- low statistics!
- back-to-back preference lower for like-sign pairs
- Statistical Model captures main features (phasespace dominates)
- Agreement improves when Bose-Einstein correlations modify phasespace
 - R=0.75 fm used [reasonable enough]

$\pi^-\pi^-$ and $\pi^+\pi^+$ pairs



$\pi^-\pi^+$ pairs



- until recently, in particle physics the “GGLP effect” is relevant mostly inasmuch as it distorts the W mass (e.g. [arXiv:hep-ph/9805223](https://arxiv.org/abs/hep-ph/9805223))
- in heavy ion physics, however, it plays a prominent role

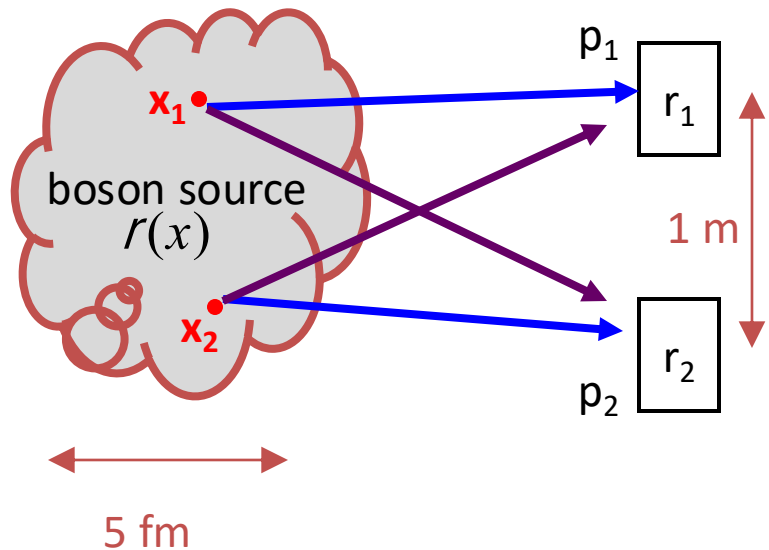


Edward Shuryak

Evolution to heavy ion collisions

- early 1970's: connection between GGLP and HBT [Shuryak, Kopylov, Podgiretsky...]

Identical non-interacting bosons



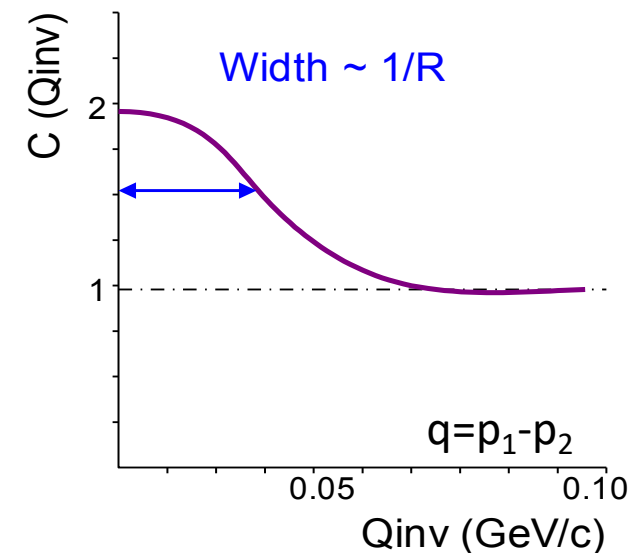
$$\Psi = \frac{1}{\sqrt{2}} \left[U(\vec{x}_1, \vec{p}_1) e^{i(\vec{r}_1 - \vec{x}_1) \cdot \vec{p}_1 / \hbar} \times U(\vec{x}_2, \vec{p}_2) e^{i(\vec{r}_2 - \vec{x}_2) \cdot \vec{p}_2 / \hbar} + U(\vec{x}_2, \vec{p}_1) e^{i(\vec{r}_1 - \vec{x}_2) \cdot \vec{p}_1 / \hbar} \times U(\vec{x}_1, \vec{p}_2) e^{i(\vec{r}_2 - \vec{x}_1) \cdot \vec{p}_2 / \hbar} \right]$$

$$\Psi^* \Psi = \underbrace{U_1^* U_1}_{\text{Prob. \#1}} \cdot \underbrace{U_2^* U_2}_{\text{Prob. \#2}} \cdot [1 + \cos((\vec{p}_1 - \vec{p}_2) \cdot (\vec{x}_1 - \vec{x}_2) / \hbar)]$$

$$C(\vec{p}_1, \vec{p}_2) \equiv \frac{P(\vec{p}_1, \vec{p}_2)}{P(\vec{p}_1)P(\vec{p}_2)} = 1 + |\tilde{\rho}(\vec{q})|^2$$

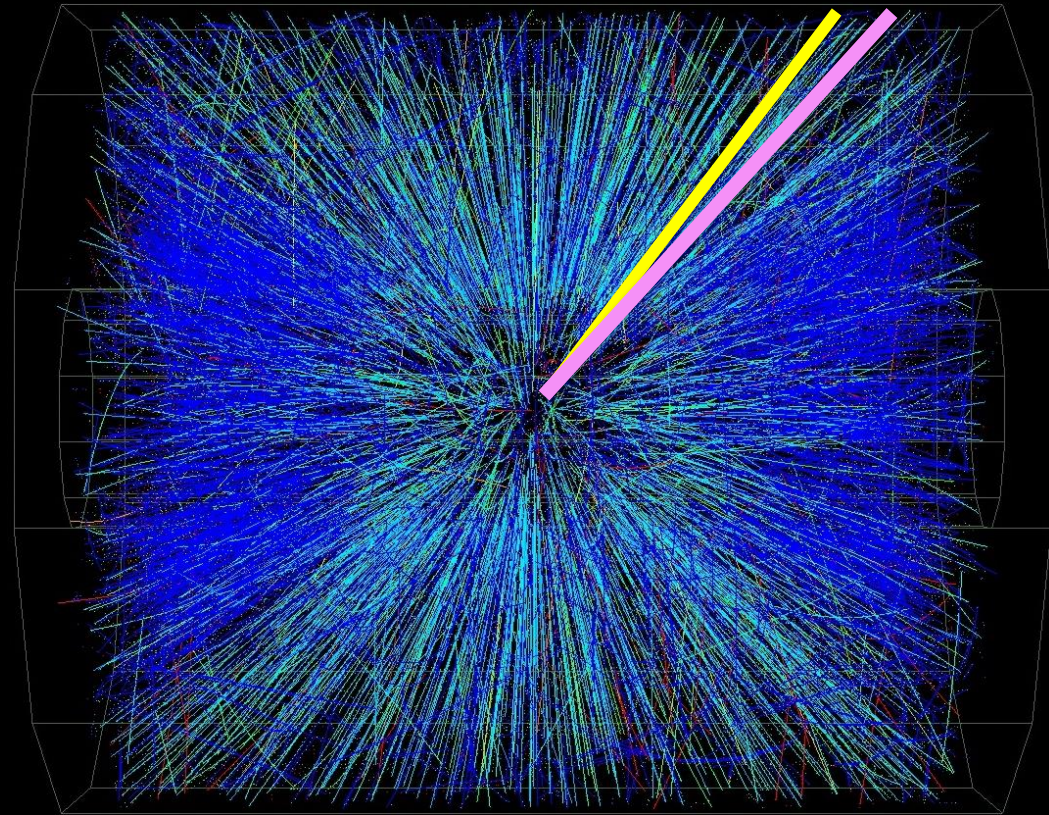
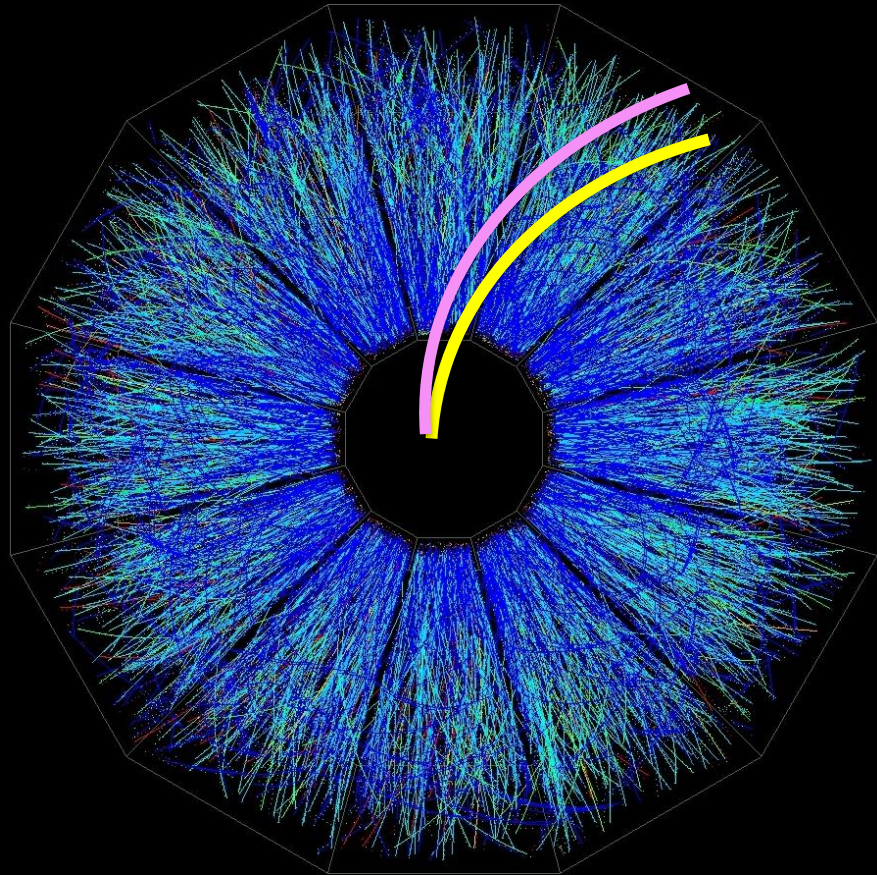
↑
Measurable

↑
F.T. of pion source

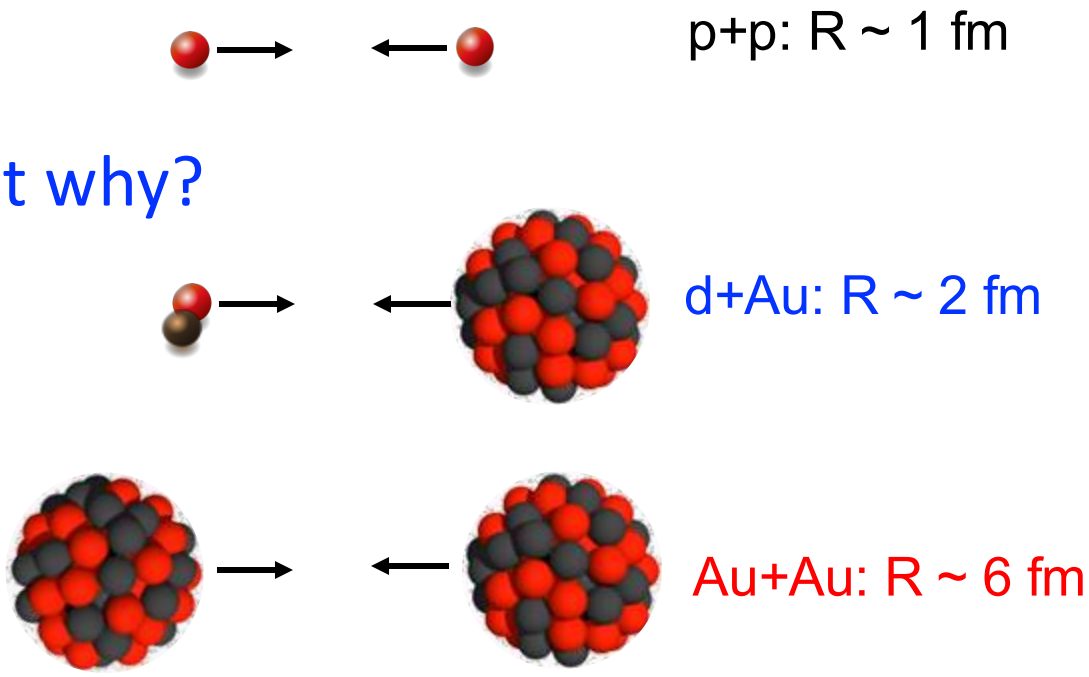
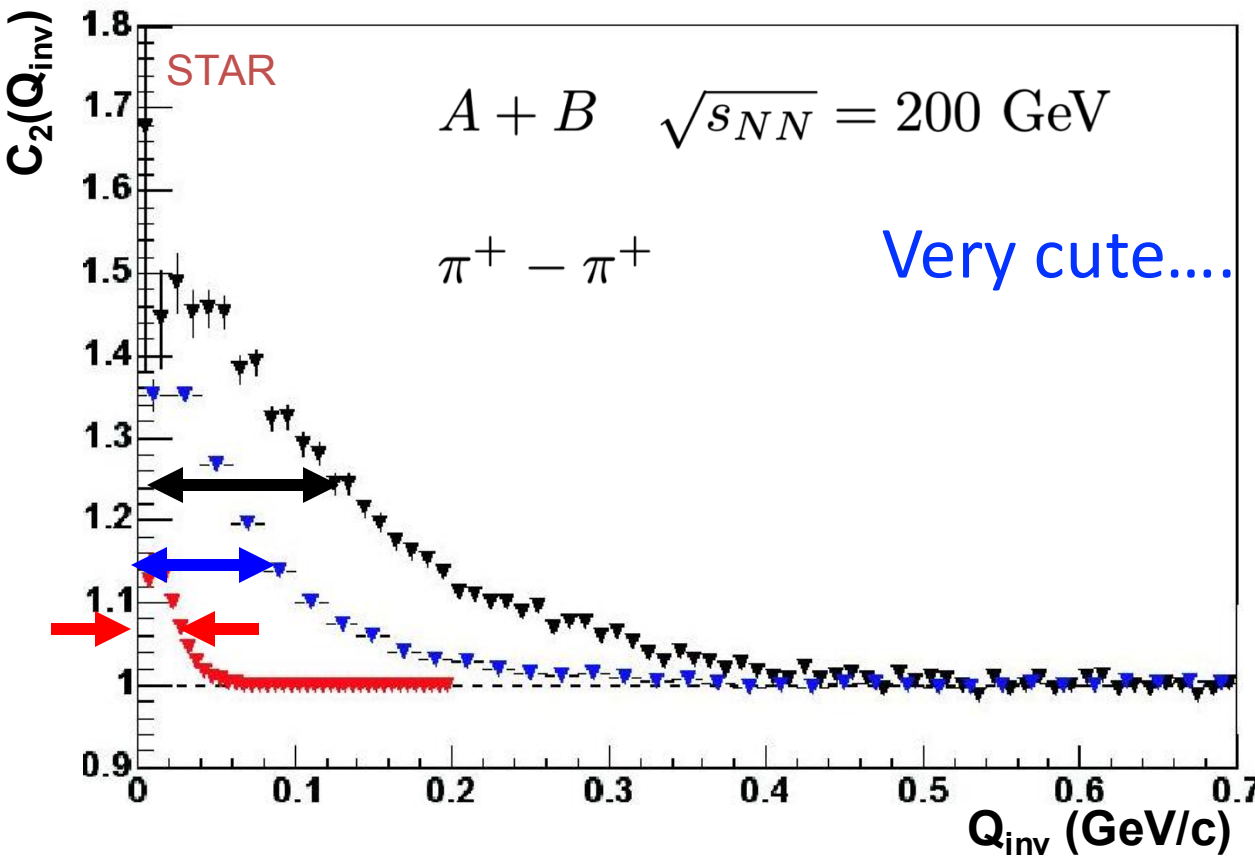


$$C(\vec{q}) = 1 + \int d^3r S(\vec{r}) \cos(\vec{q} \cdot \vec{r}) = \frac{N(\vec{p}_1, \vec{p}_2)}{N_{\text{mix}}(\vec{p}_1, \vec{p}_2)} \leftarrow \begin{array}{l} \text{dominated by phasespace} \\ \text{MUCH more complicated than SII} \end{array}$$

Correlation expresses a conditional probability (~SII)

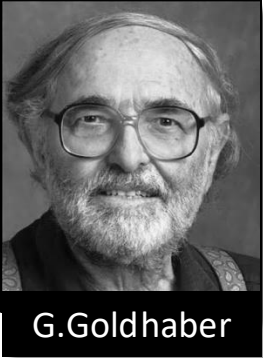


Sanity check: Intensity Interferometry for 3 systems



GGLP → Femtoscopy in heavy ion collisions

- 1960: GGLP observe small correlation between identical pions in p-pbar annihilation. Largely a curiosity



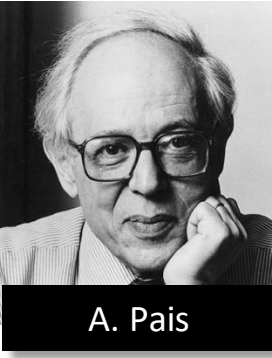
G. Goldhaber



S. Goldhaber



W. Lee



A. Pais



Edward Shuryak

- early 1970's: connection between GGLP and HBT [Shuryak. Kopylov, Podgiretsky...]

- late 1970's – early 1980's: explosive development in **new field of heavy ion collisions**



Miklos Gyulassy



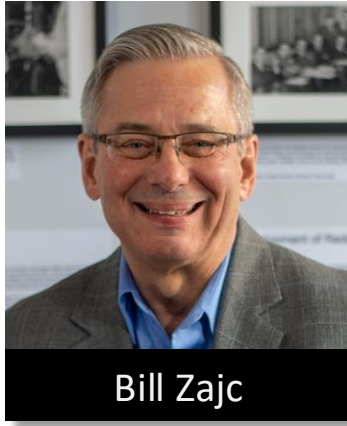
Steve Koonin



Scott Pratt



Richard Lednicky



Bill Zajc



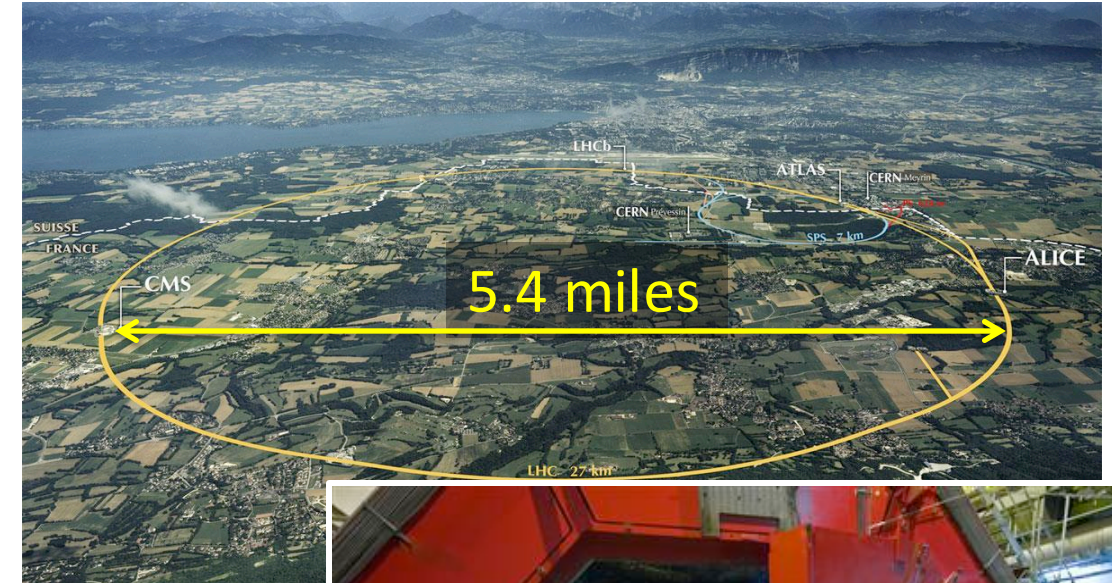
Laura Fabbietti

...

Relativistic Heavy Ion Collider (RHIC) Brookhaven Lab, NY, USA

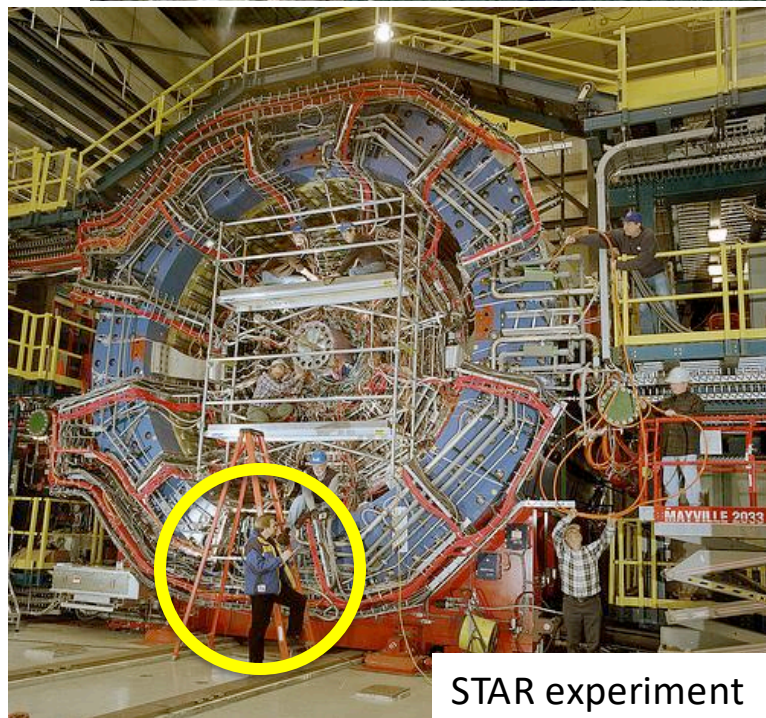


Large Hadron Collider (LHC) CERN, France/Switzerland

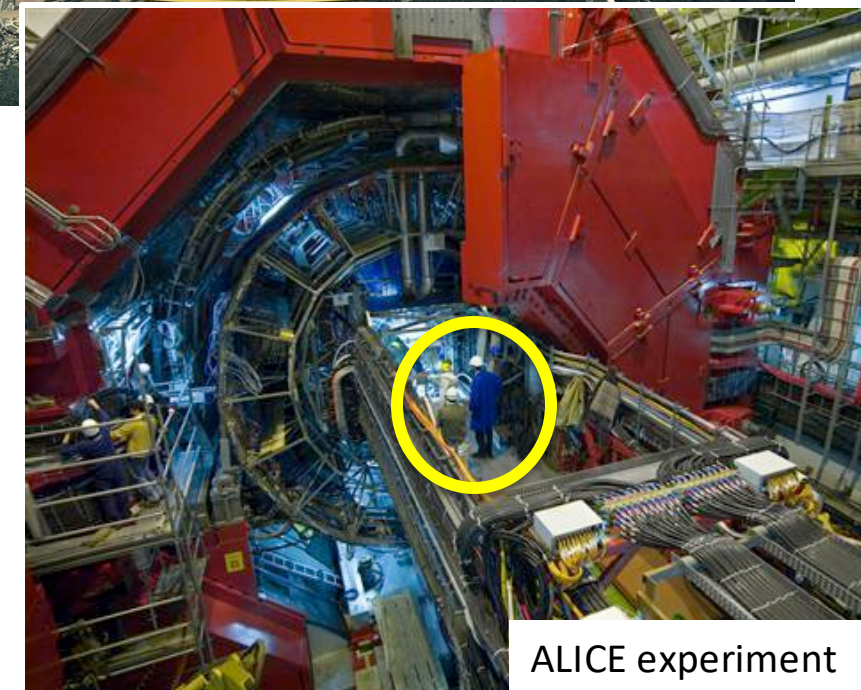


Ultrarelativistic collisions of:

- p+p
- Au+Au / Pb+Pb
- (and p+Au, Cu+Cu, etc.)

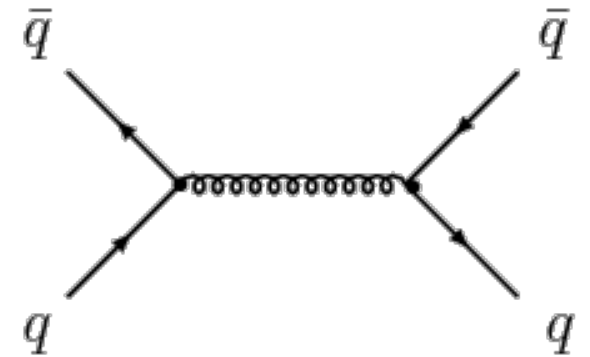
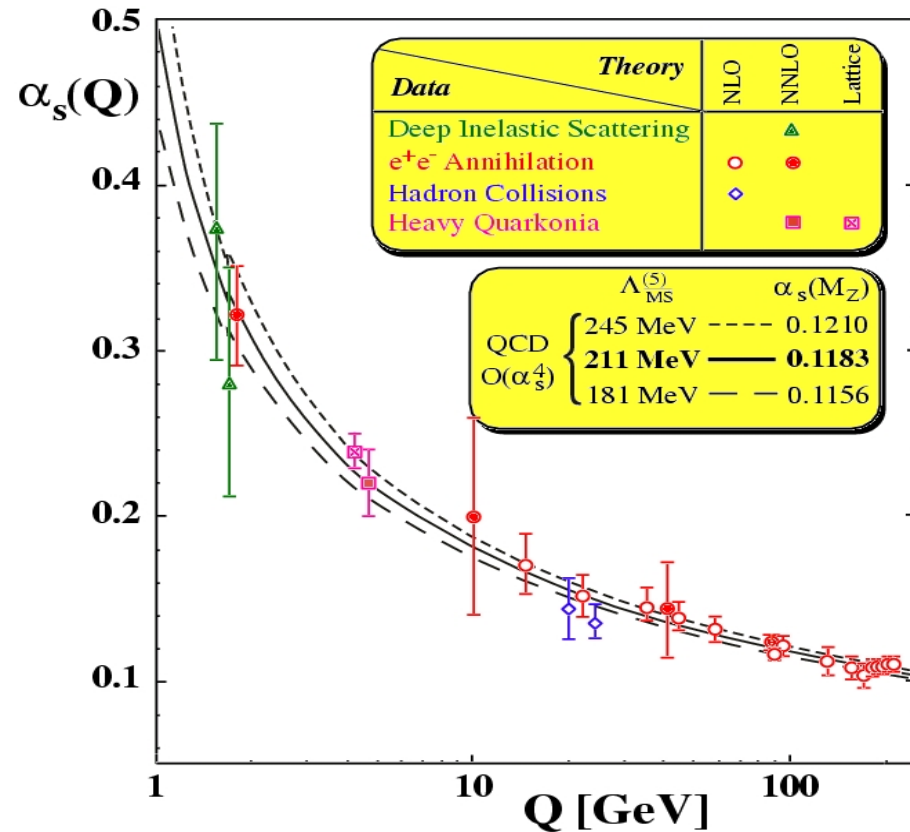
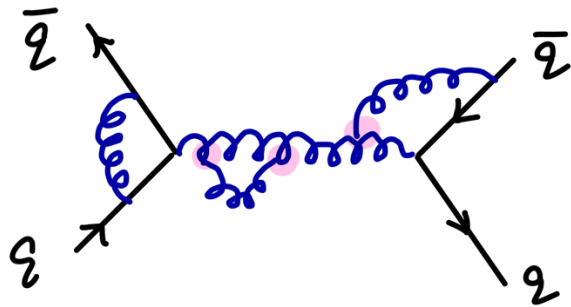


STAR experiment



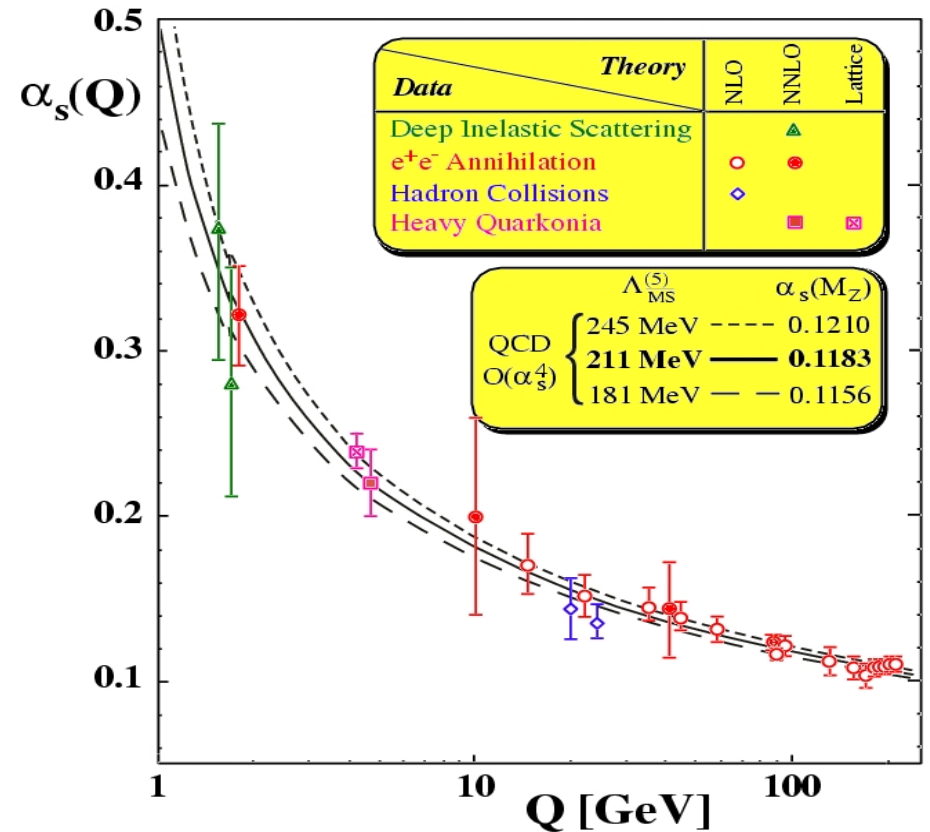
ALICE experiment

- Theory of Strong Force between quarks: Quantum Chromodynamics (QCD)
- Strength of the Strong Force depends on momentum transfer (spatial scale)
- Complicated & least-well-understood interaction



“Running” of the QCD coupling constant

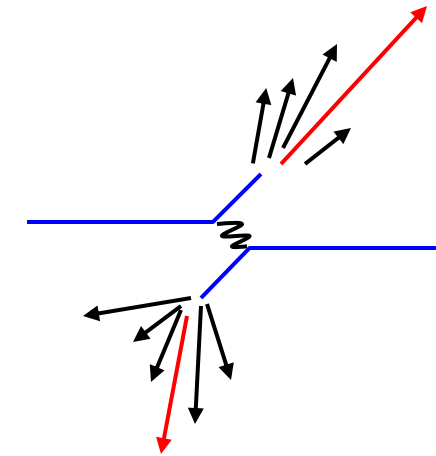
Particle Physics



focus on **fundamental particles**

Large Q : **Asymptotic Freedom**

- reduce “messy” QCD effects
- perturbative calculations work

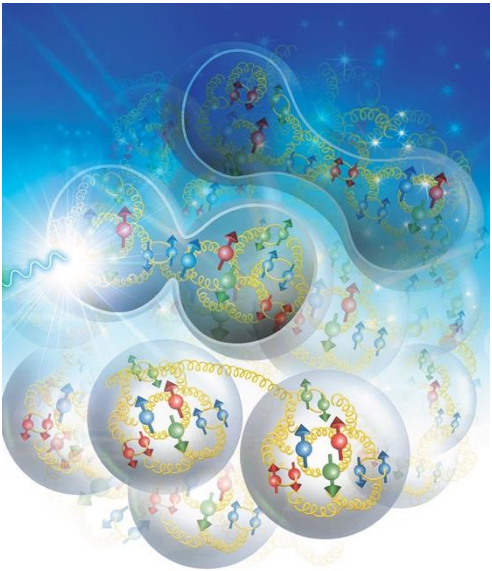


- ✓ Smaller/simpler is better
- ✓ More energy is better

Heavy Ion Physics

Low Q: **Confinement**

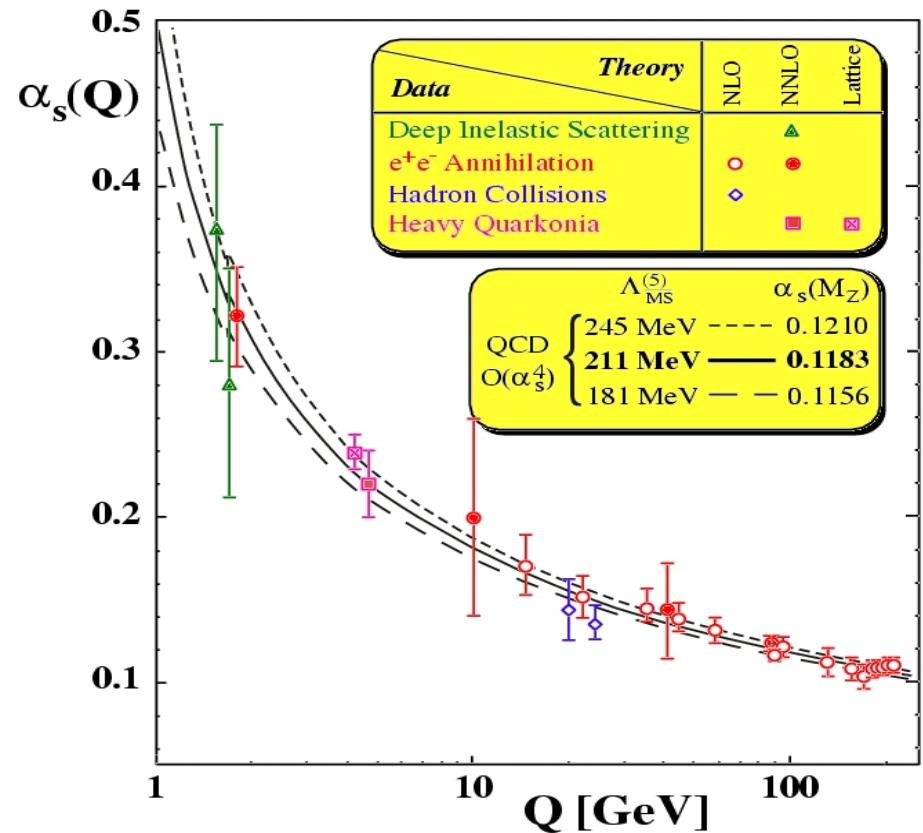
- dominates mass in universe
- theoretical insight limited



intrinsic scales of QCD →

- ✓ optimum energy range
- ✓ bigger is better ($\gg 1$ fm)

focus on **fundamental interaction**

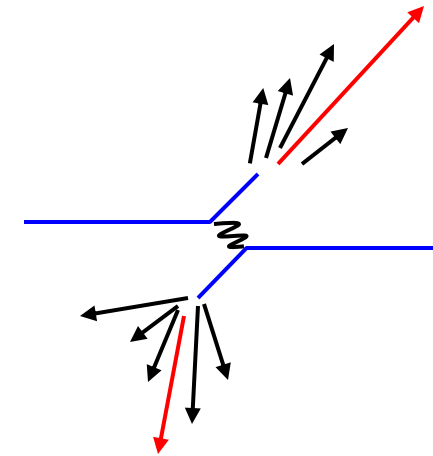


focus on **fundamental particles**

Particle Physics

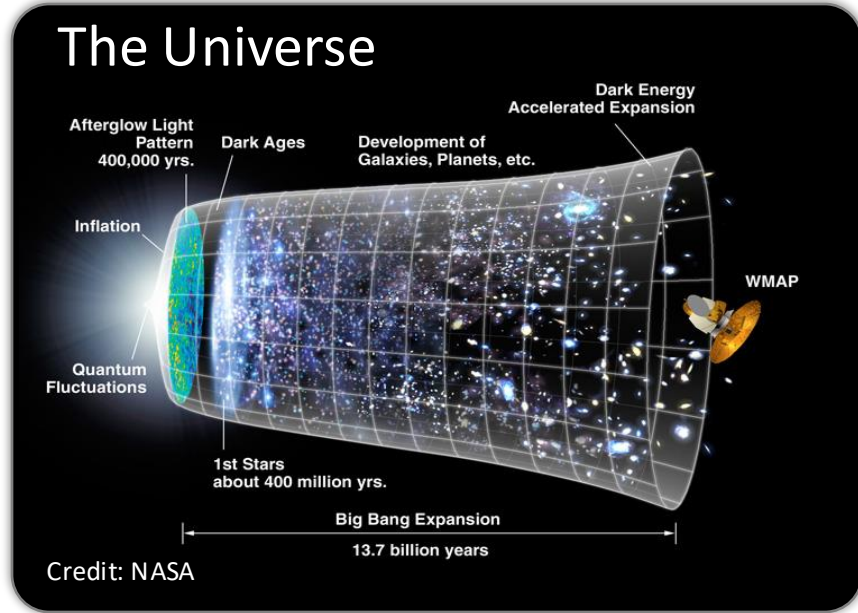
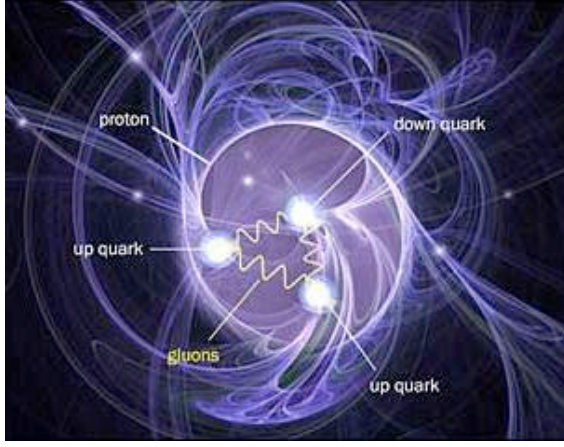
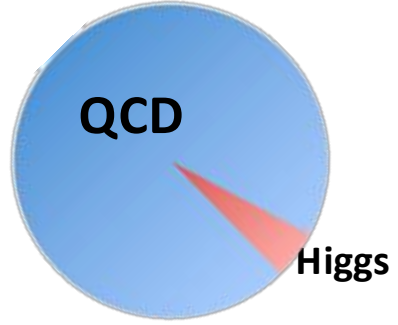
Large Q : **Asymptotic Freedom**

- reduce “messy” QCD effects
- perturbative calculations work



- ✓ Smaller/simpler is better
- ✓ More energy is better

Deconfinement transition

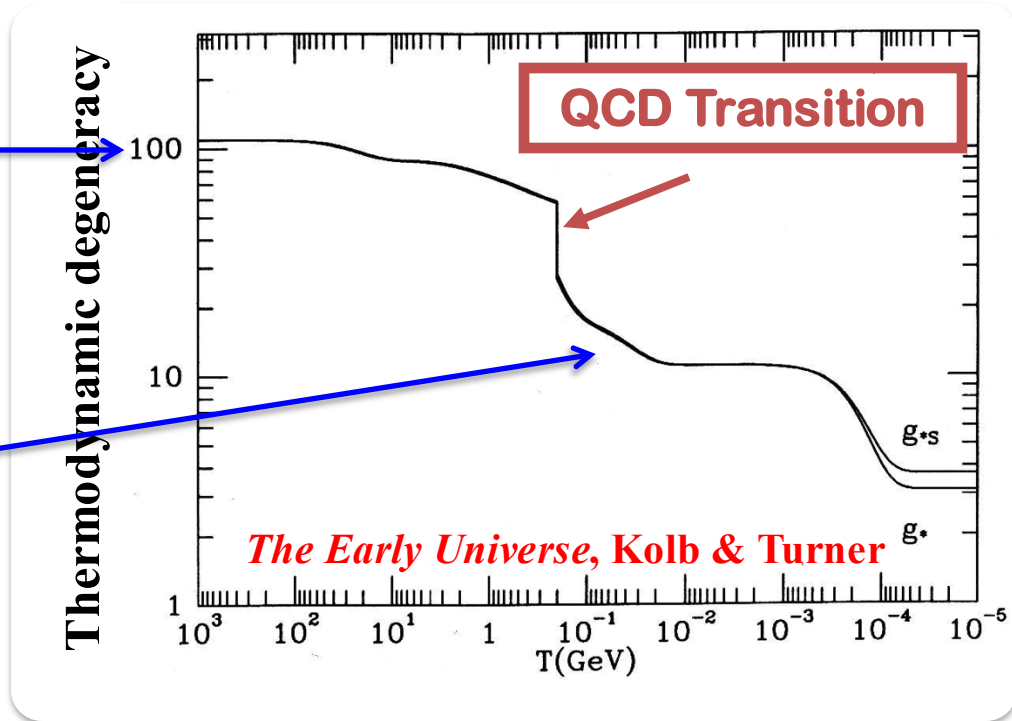


Deconfined color charges
Quark-gluon plasma
 • first $\sim 3 \mu s$ after Big Bang

A cluster of small, multi-colored dots representing deconfined quarks and gluons in a plasma state.

Color confined inside
 net-color-neutral **hadrons**
 (e.g. proton)

A cluster of larger, multi-colored spheres representing hadrons where quarks and gluons are confined together.

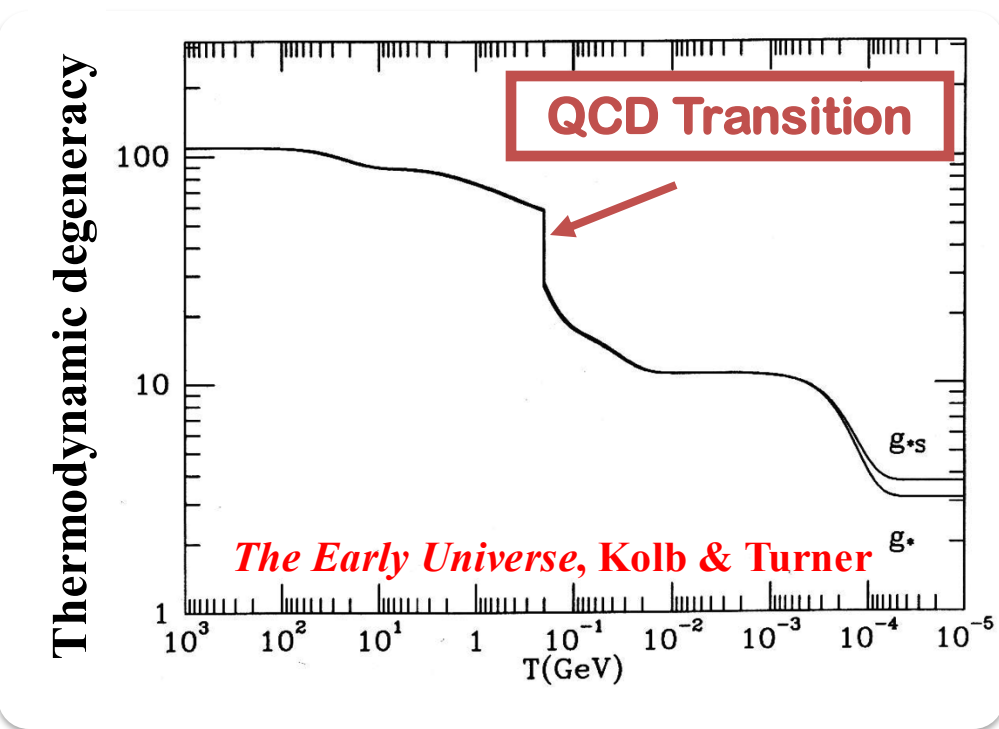
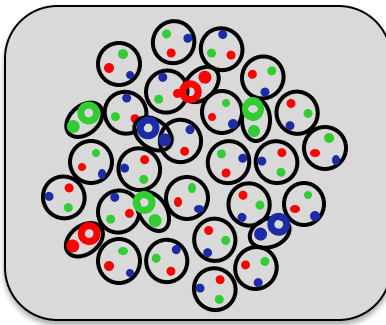
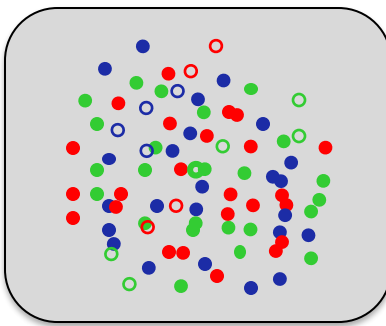
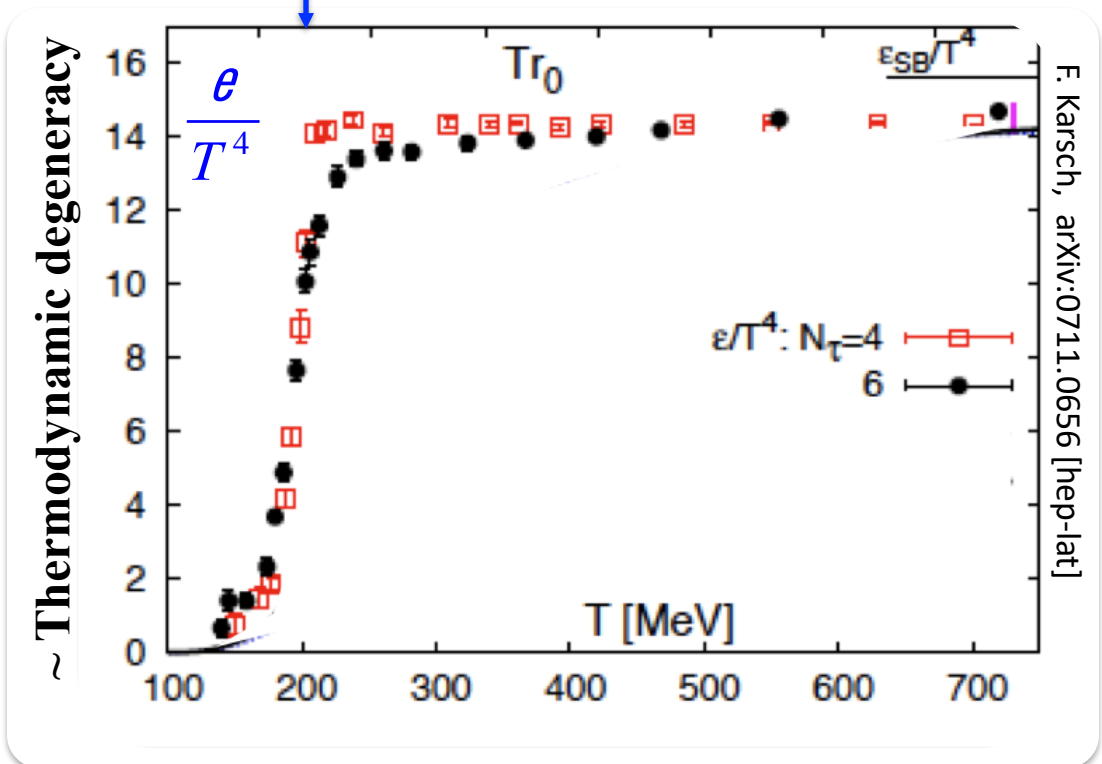
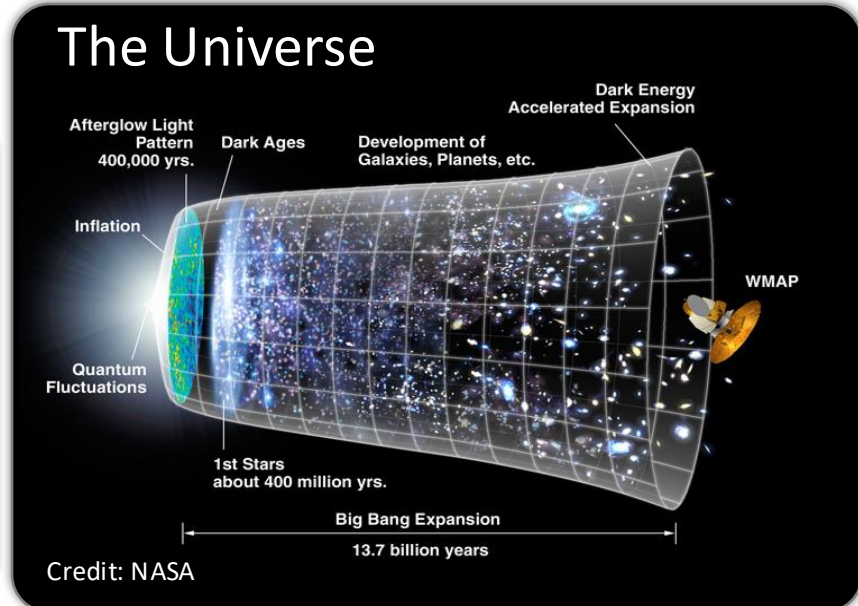
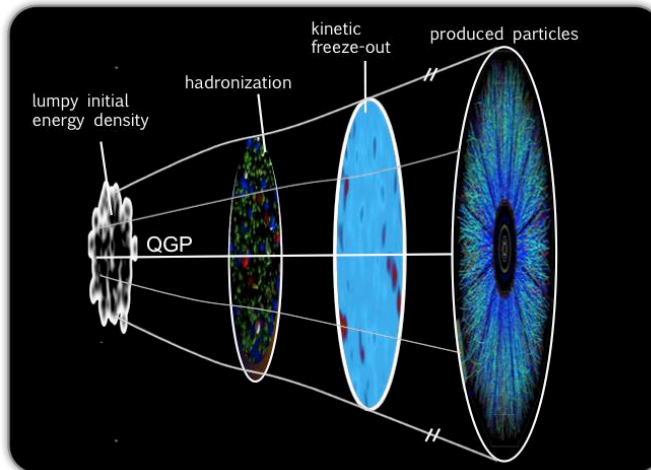


Deconfinement transition

Lattice QCD calculation:

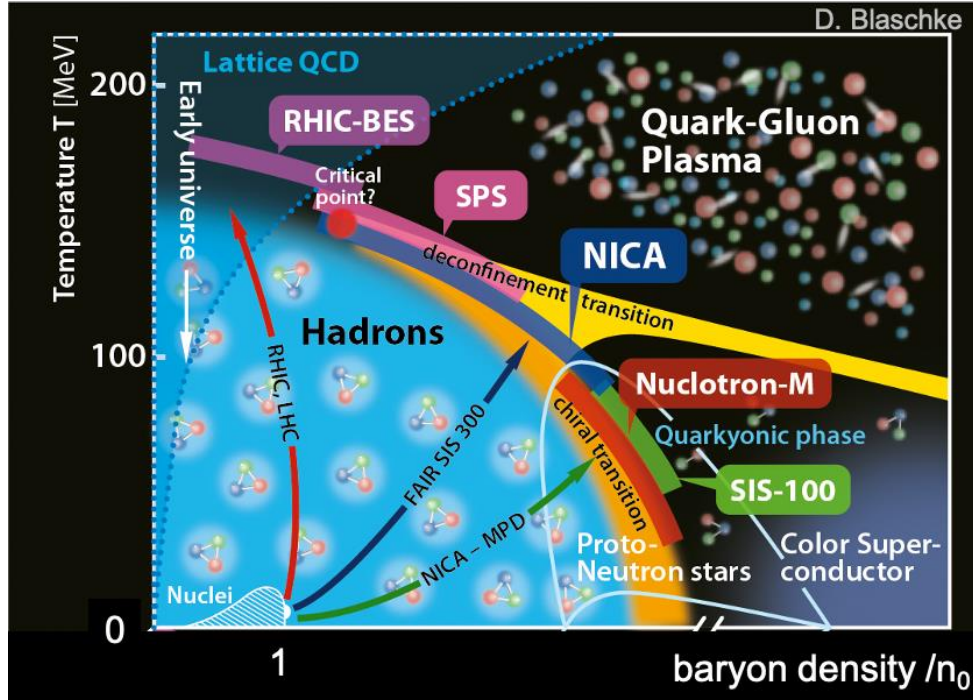
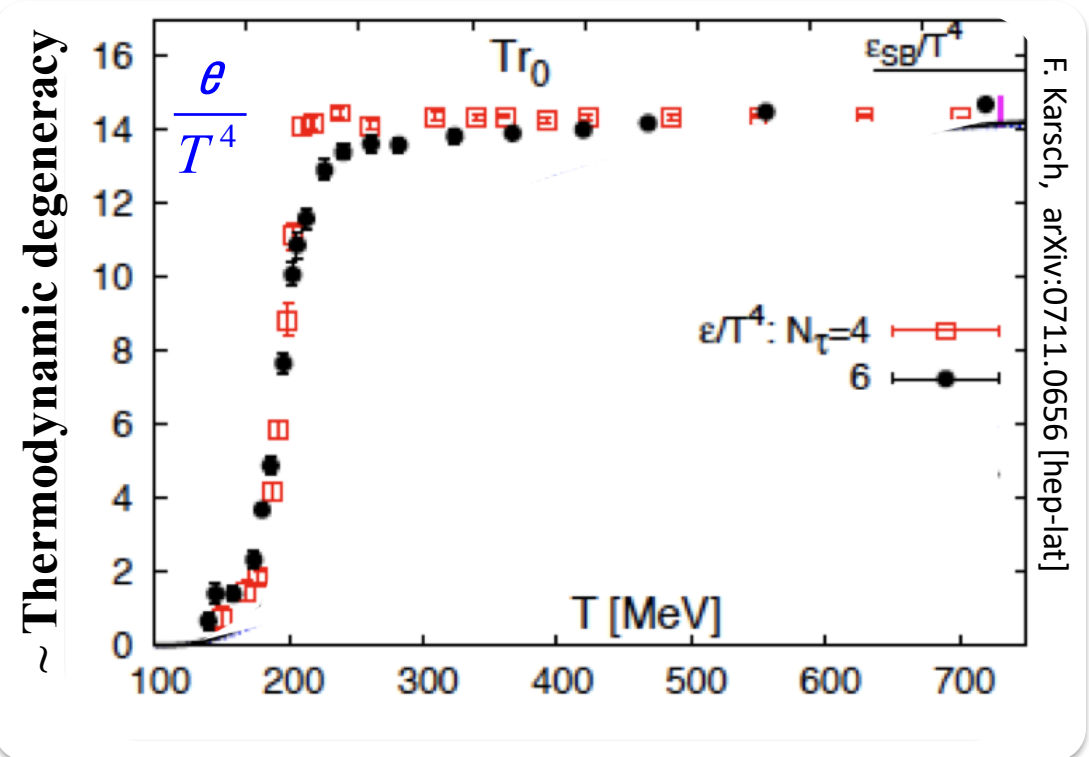
- $T < 150 \text{ MeV} \rightarrow$ interacting hadrons
- $T > 150 \text{ MeV} \rightarrow$ deconfined quarks

$$150 \text{ MeV} = 2 \times 10^{12} \text{ K} \sim 10^5 T_{\odot}$$

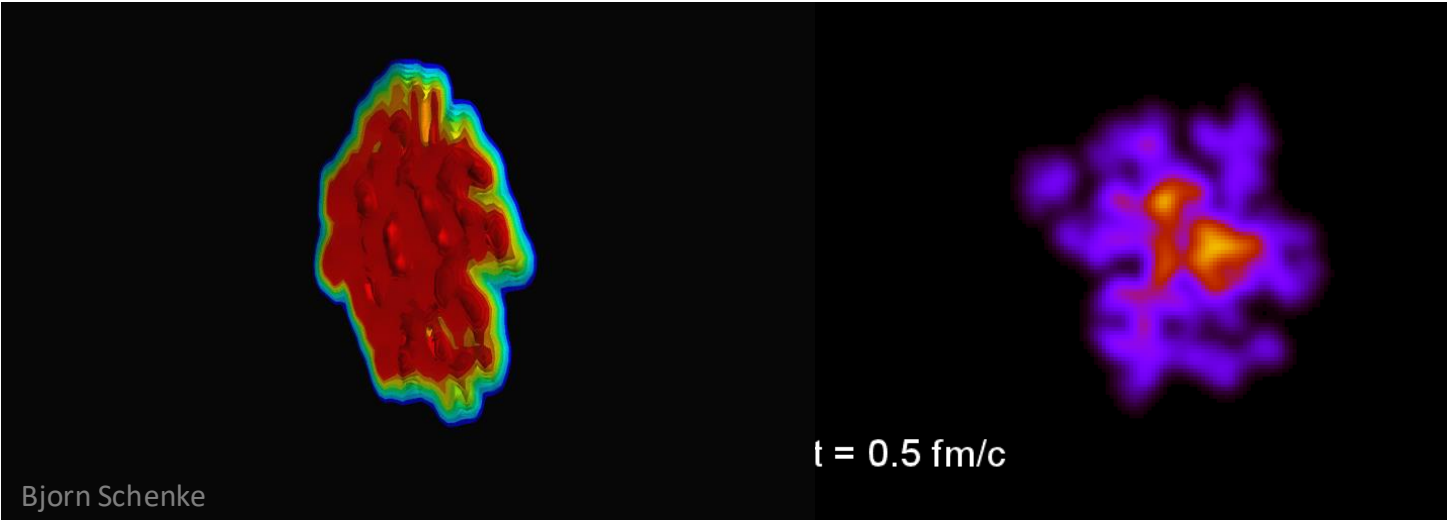


Equation of state – characterizing bulk matter

Lattice QCD calculation:



Equation of state – driving dynamic evolution



The New York Times

At One Trillion Degrees, Even Gold Turns Into the Sloshiest Liquid

By Kenneth Chang

April 19, 2005



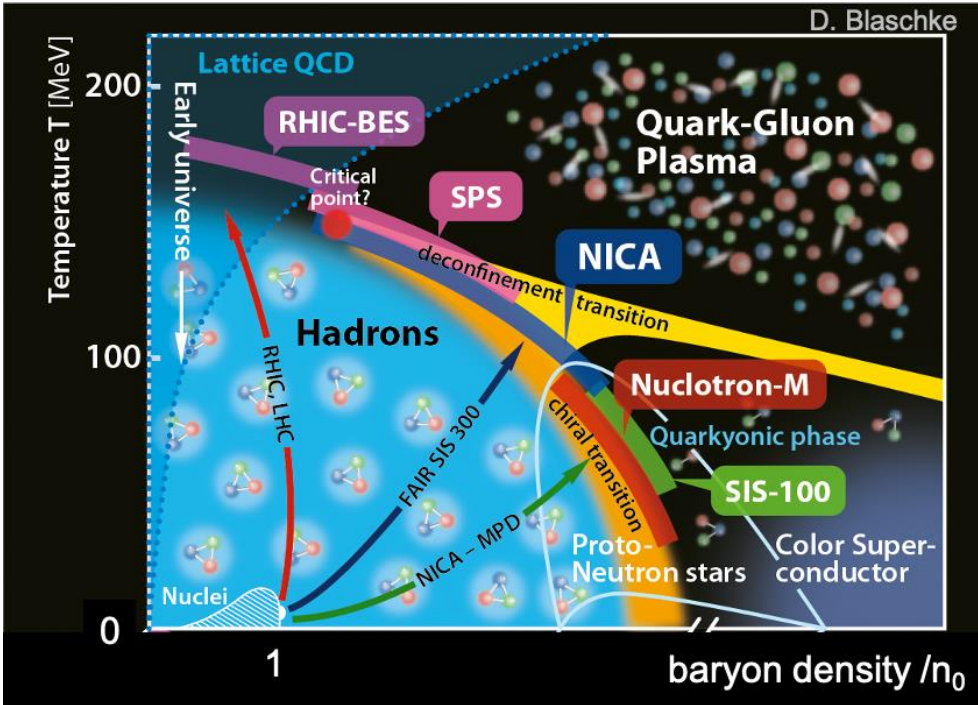
RHIC serves the perfect fluid

From a (lumpy) initial state, solve hydro equations:

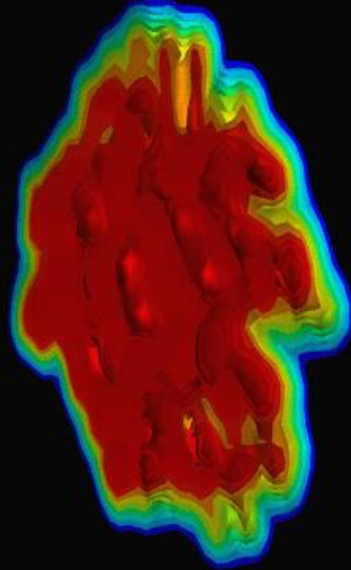
$$d_m T^{mn} = 0 \quad T^{m,n} = eu^m u^n - (p + P) D^{mn} + \rho^{mn}$$

$$u^m d_m P = -\frac{1}{t_p} (P + zq) - \frac{1}{2} P \frac{zT}{t_p} d_l \left(\frac{t_p}{zT} u^l \right)$$

& the equation of state



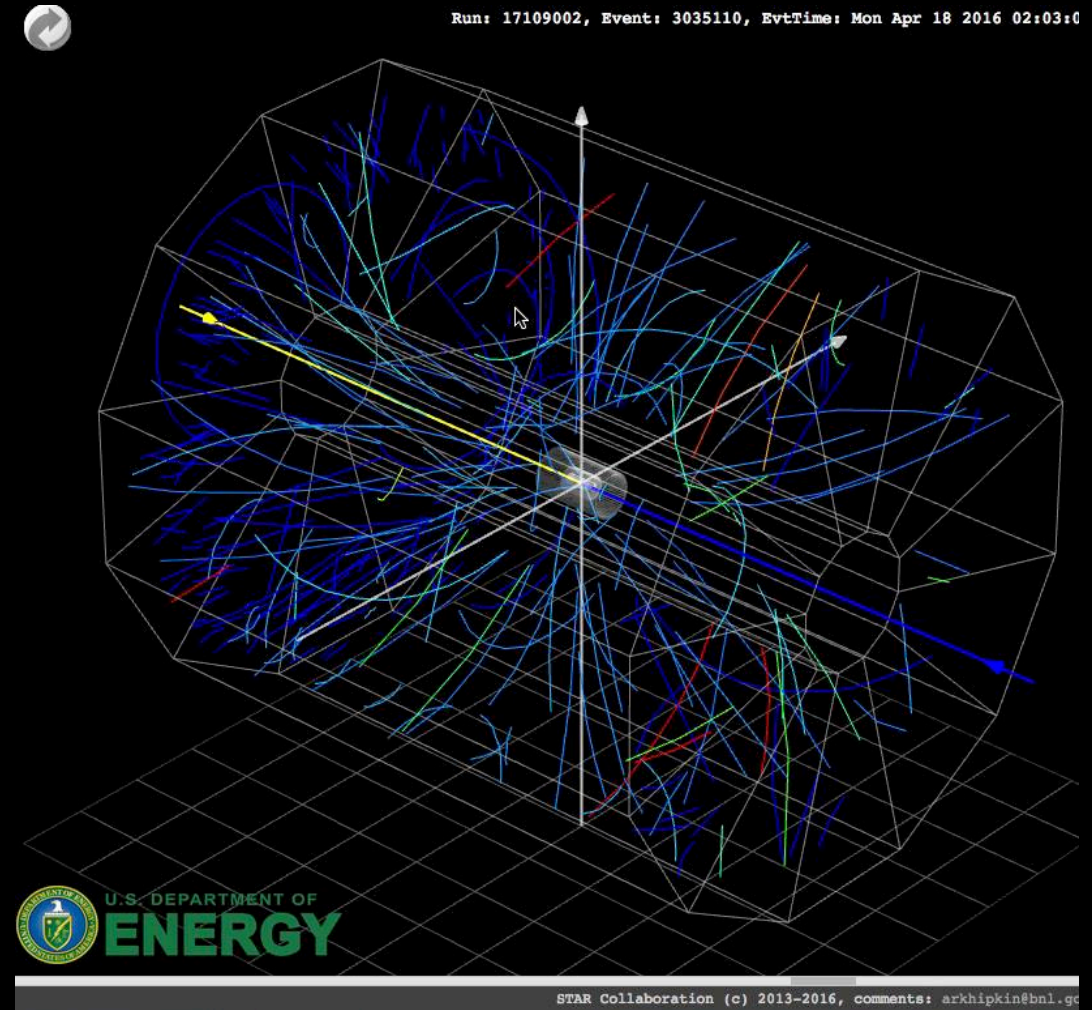
Femto-scale simulation



Bjorn Schenke

- Detectors record identities and *momenta* of emitted hadrons
- No direct spacetime information
 - “angular diameter” ~ **nanoarcsecond**
- Two-hadron intensity interferometry (femtoscopy) is crucial

Macro-scale reality

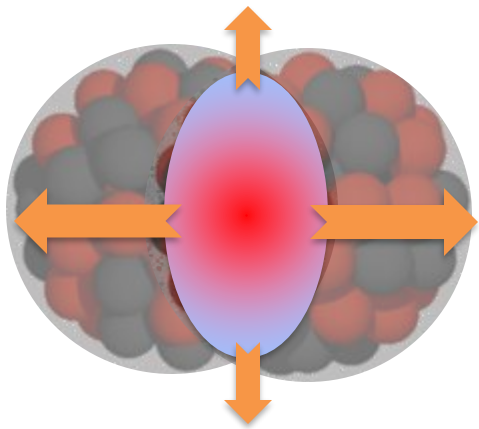


STAR Collaboration (c) 2013-2016, comments: arkhipkin@bnl.gov

Geometry – the hallmark of heavy ion physics

- Size matters – need a *bulk* system
- Shape matters – anisotropic geometry key

degenerate fermi gas (supercooled ${}^6\text{Li}$)
released from anisotropic magnetic trap

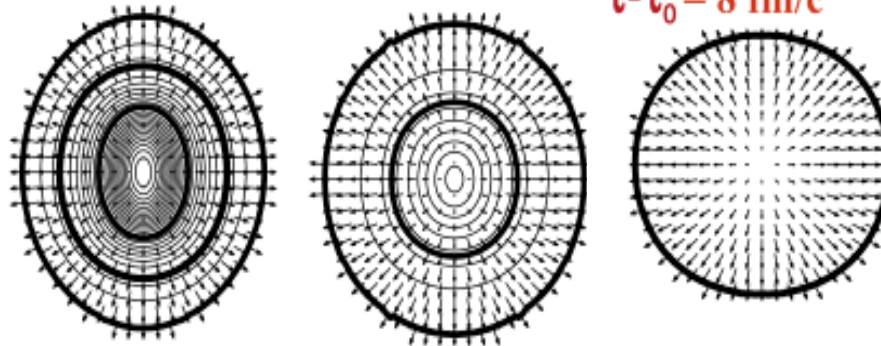


$\tau - \tau_0 = 3.2 \text{ fm}/c$

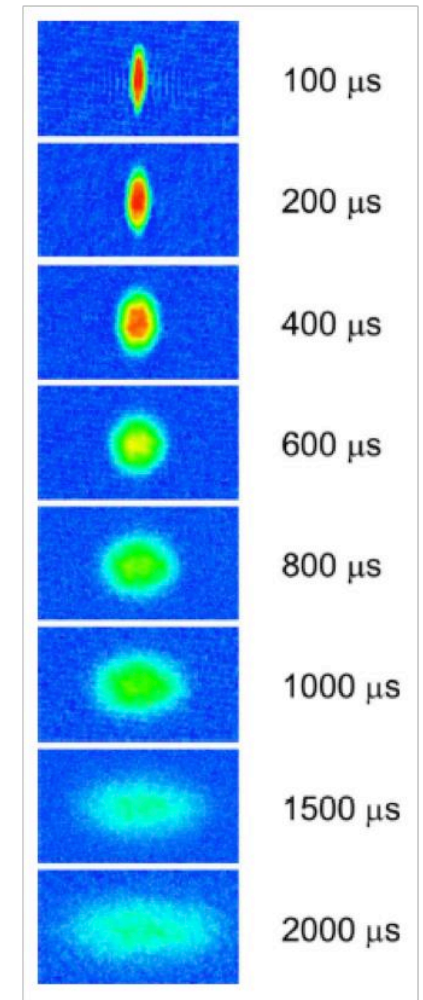


hydro calculations: Kolb & Heinz

$\tau - \tau_0 = 8 \text{ fm}/c$



- “Elliptic flow” driven by anisotropic pressure gradients: sensitive to E.o.S. & viscosity
- universally observed for strongly-interacting systems

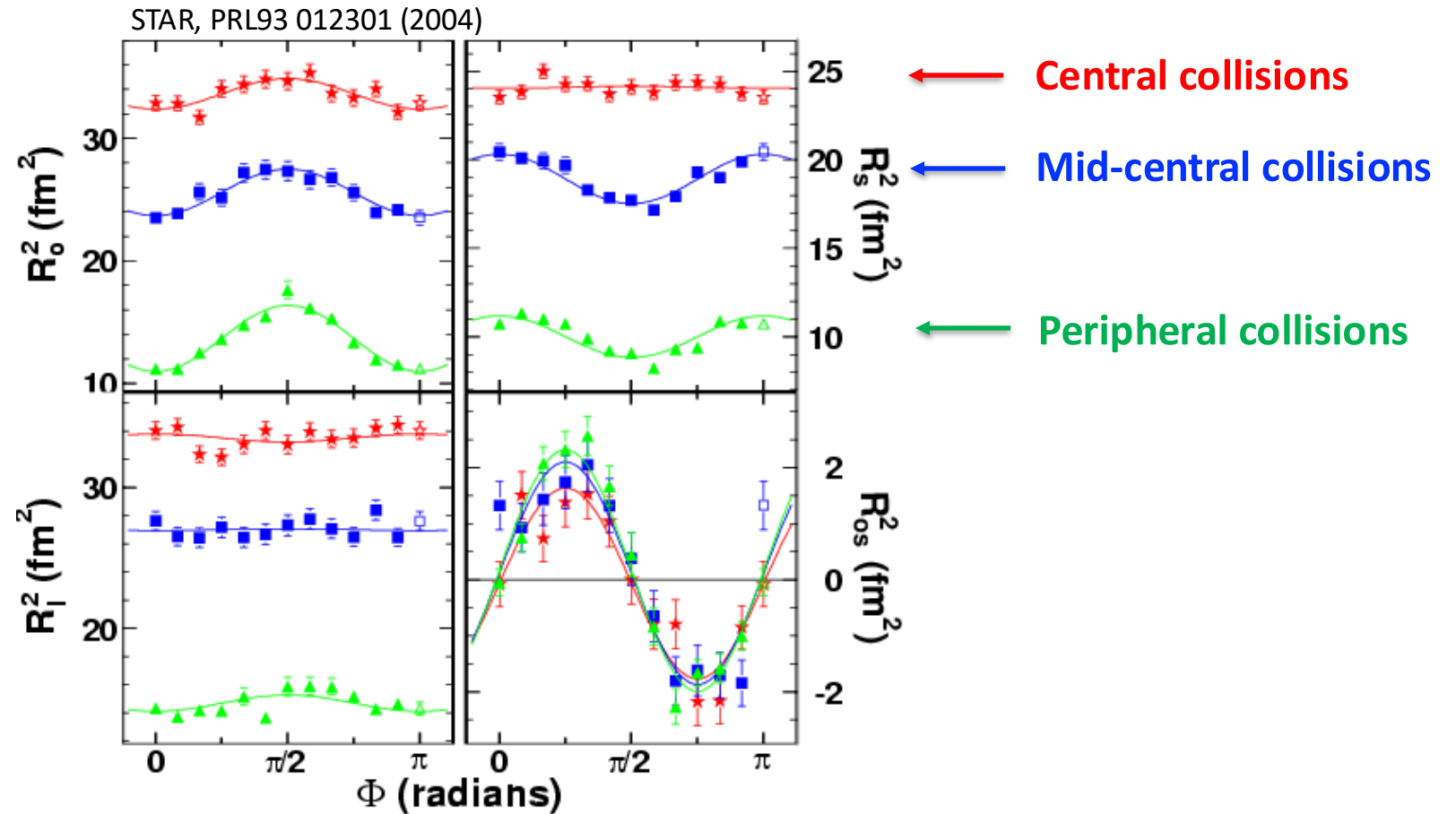
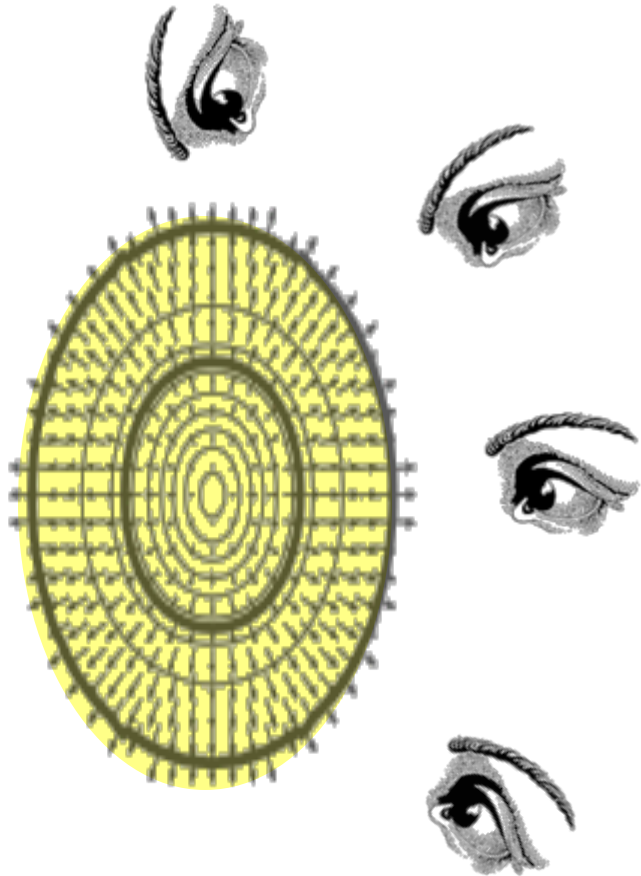


O'Hara et al, *Science* 2002

Spatial aspects of elliptic flow

- Size matters – need a *bulk* system
- Shape matters – anisotropic geometry key

complementary spatial information
tightens constraints on hydro transport



Geometry – the hallmark of heavy ion physics

- Size matters – need a *bulk* system
- Shape matters – anisotropic geometry key
- Substructure matters

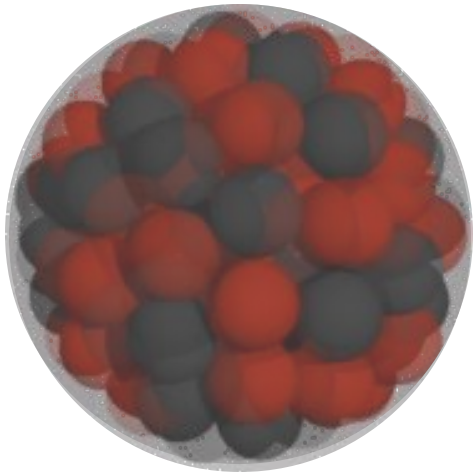
Intensity interferometry probes spacetime substructure in subatomic collisions



Geometric substructure

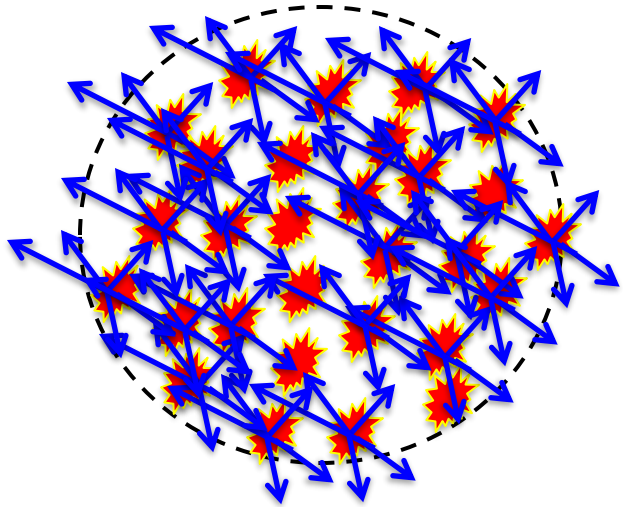
What type of system is formed?

Indeed, *is* it a system?



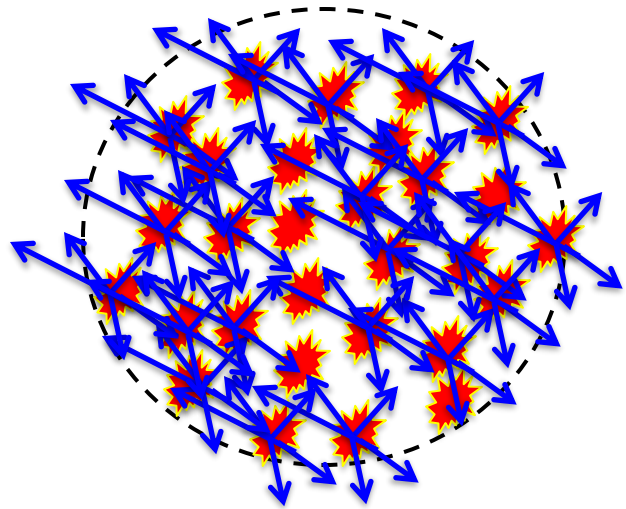
Geometric substructure

Size Independent of momentum



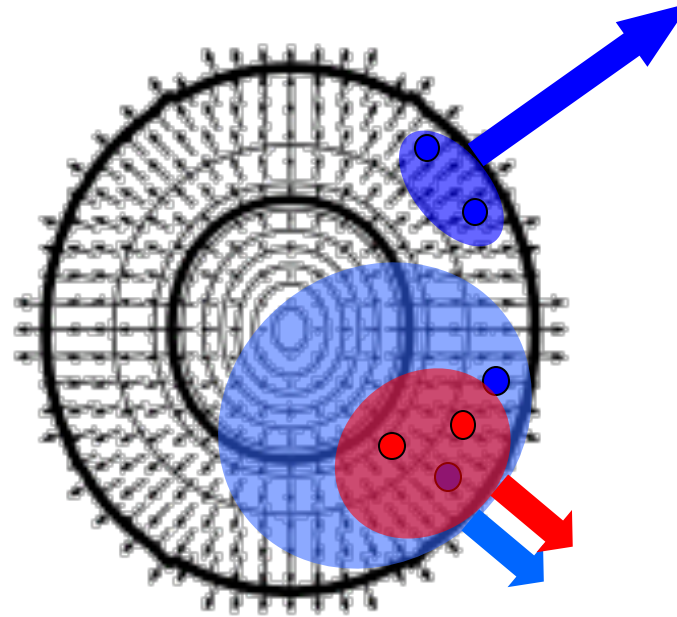
A collection of nearby, **independent**
p+p collisions. **Not “matter”**

Geometric substructure



A collection of nearby, **independent** p+p collisions. **Not "matter"**

Hydrodynamic expectation:



- pion
- kaon

Matter is characterized by fields of **bulk** properties



selecting fast particles



selecting slow particles

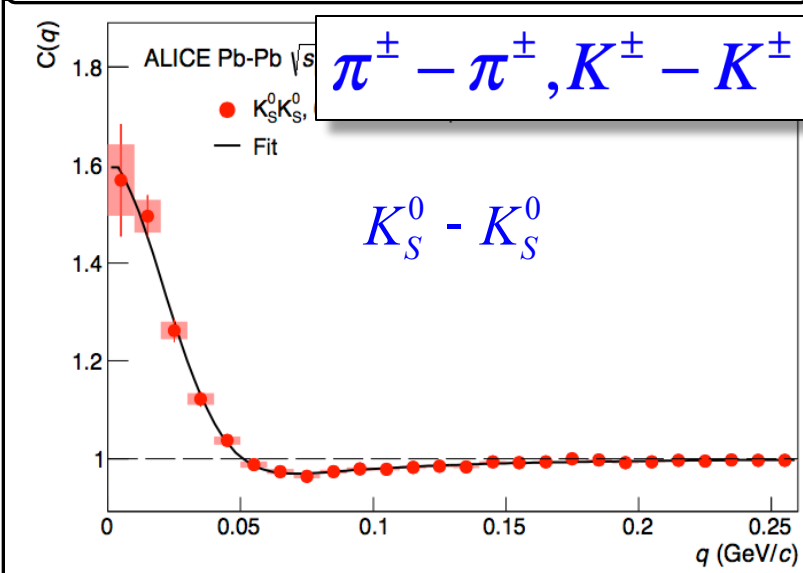
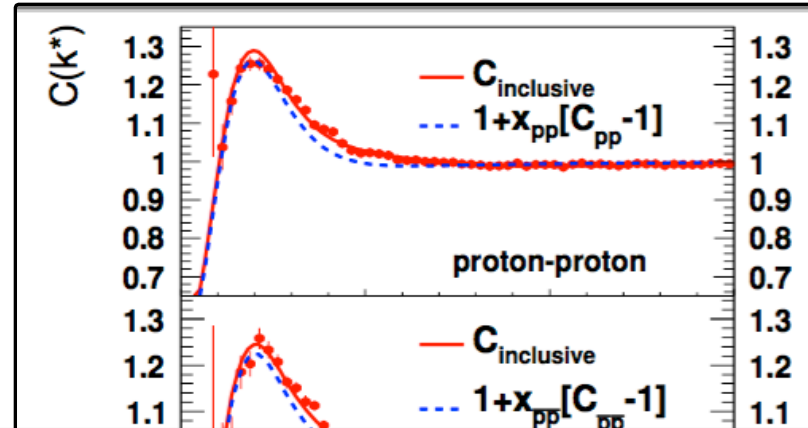
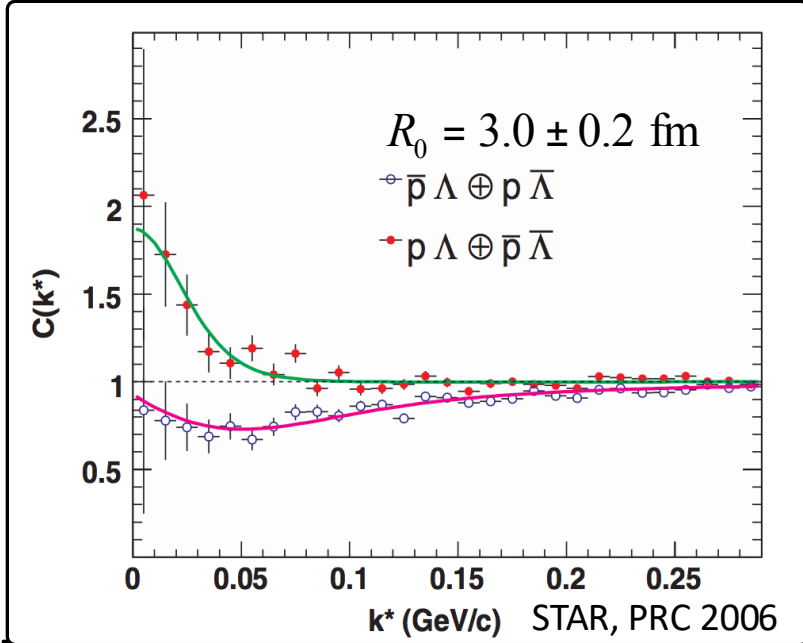
Beyond pions

$$C(\vec{q}) = \int d^3r S(\vec{r})(1 + \cos(\vec{q} \cdot \vec{r})) \leftarrow \text{non-interacting bosons}$$

$$C(\vec{q}) = \int d^3r S(\vec{r}) |\phi(\vec{q} \cdot \vec{r})|^2 \leftarrow \text{in general (Koonin-Pratt eq.)}$$

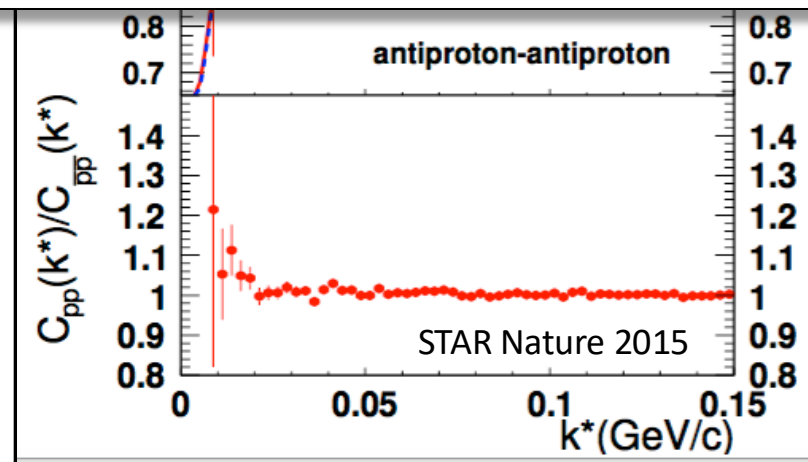
$\phi(\vec{q}, \vec{r})$ = rel. wavefunction in pair c.m. including:

- (anti)symmetrization (for identical particles)
- final-state interactions



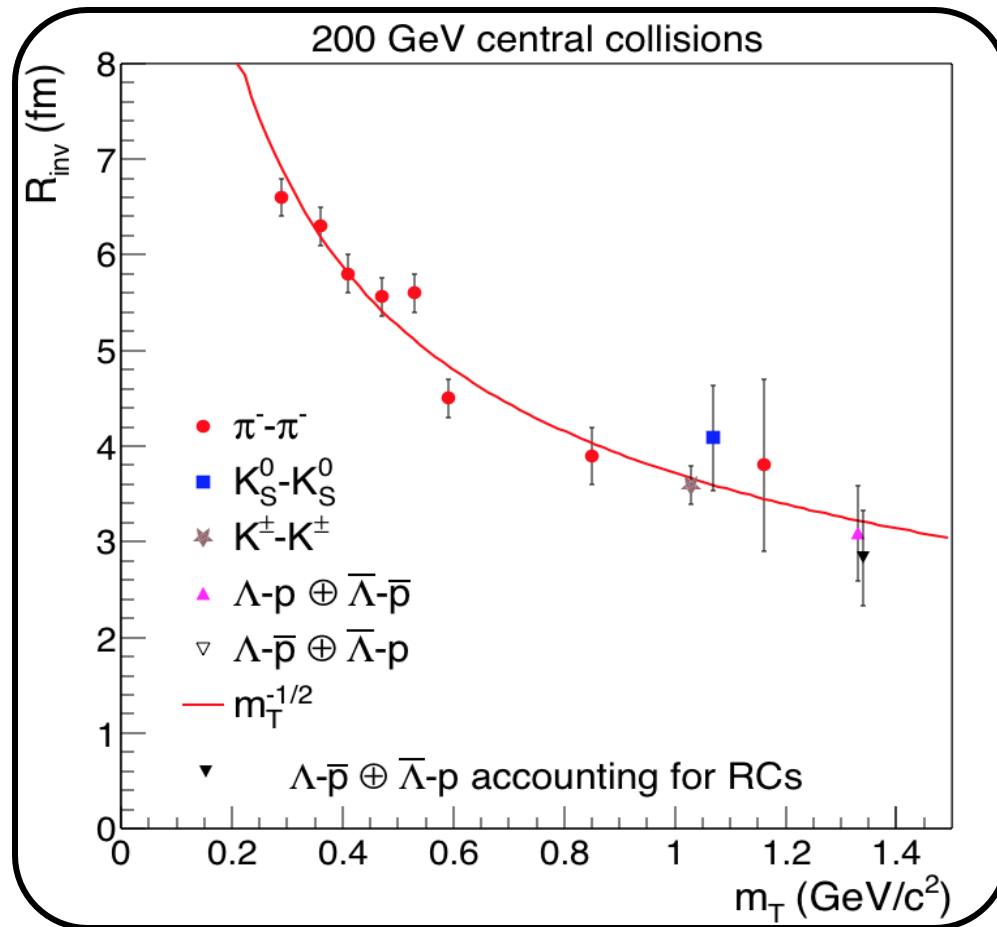
$\pi^\pm - \pi^\pm, K^\pm - K^\pm, K_S^0 - K_S^0, p - p, \bar{p} - \bar{p}, \Lambda - \Lambda, K^\pm - \pi^\pm, p - \Lambda, \Xi - \pi \dots$

$K_S^0 - K_S^0$

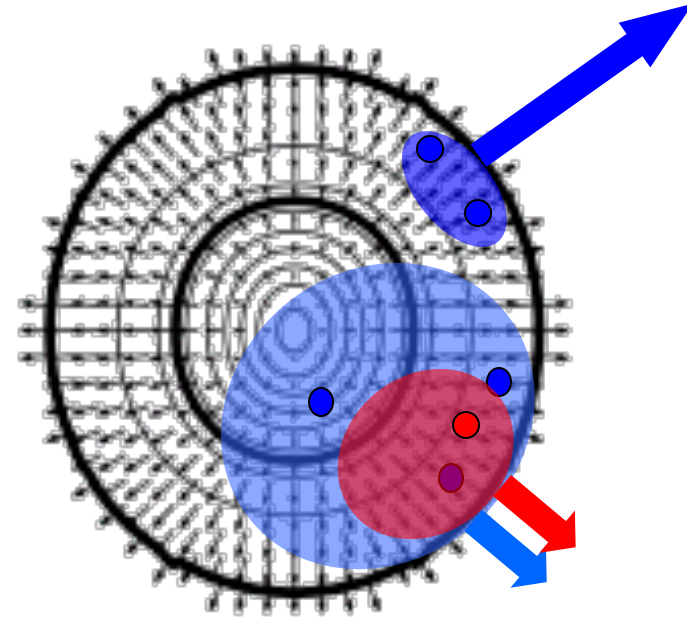


Geometric substructure

Sizes for particles of different momentum & mass



Hydrodynamic expectation:



Matter is characterized by fields of **bulk** properties

\bullet pion

\bullet kaon

Geometric substructure

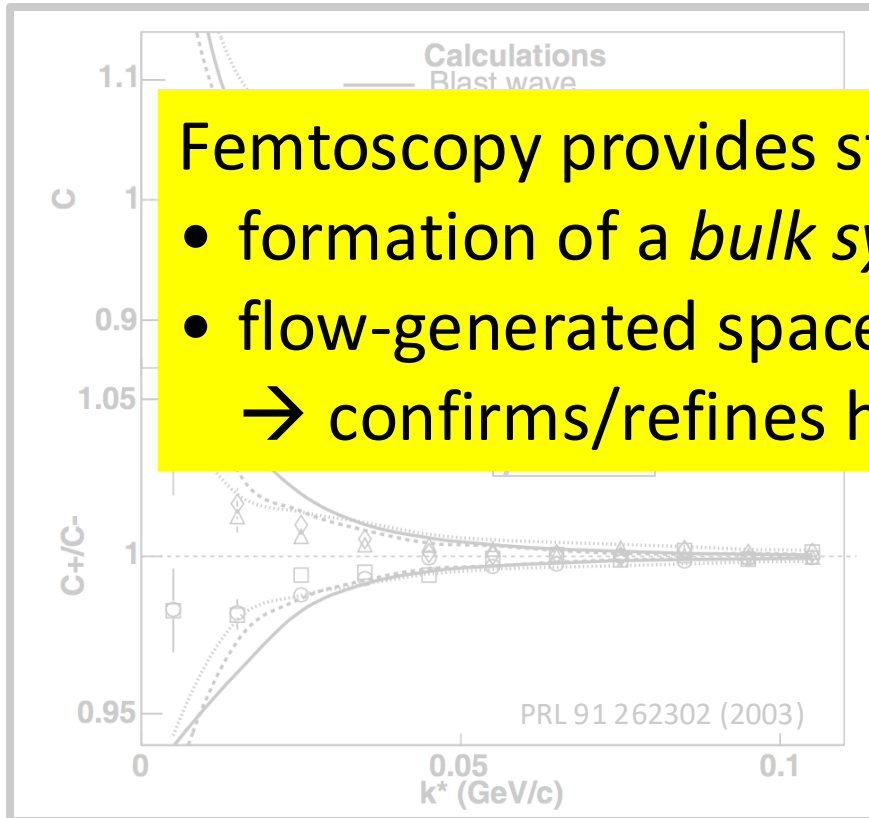
$\rho^\pm - K^\pm$ correlations reveal mass-ordered separation

Hydrodynamic expectation:

Femtoscscopy provides strong evidence for

- formation of a *bulk system*
- flow-generated space-momentum correlations

→ confirms/refines hydro treatment → access to EoS



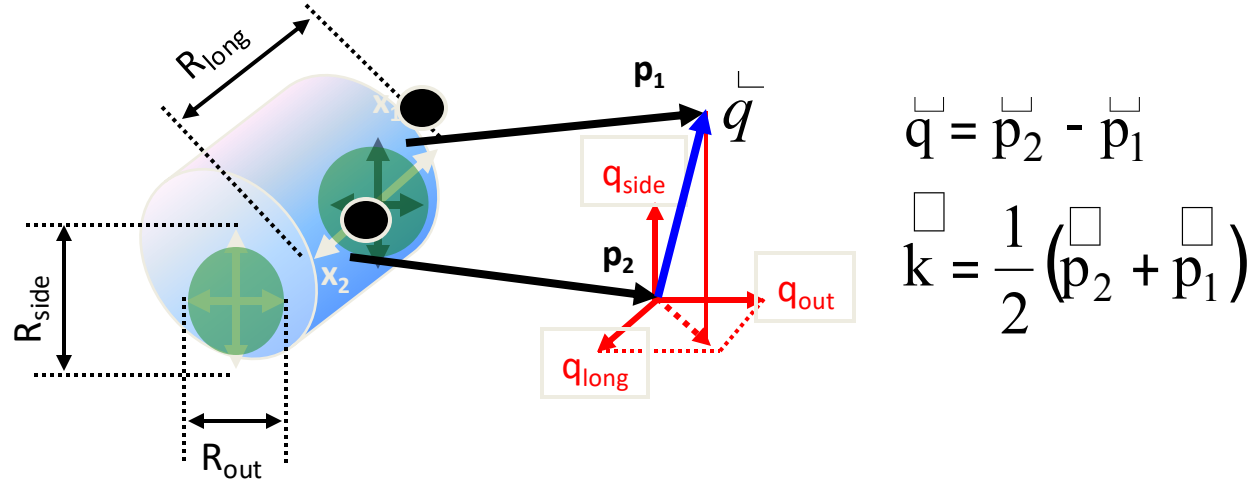
Matter is characterized by fields of **bulk** properties

● pion

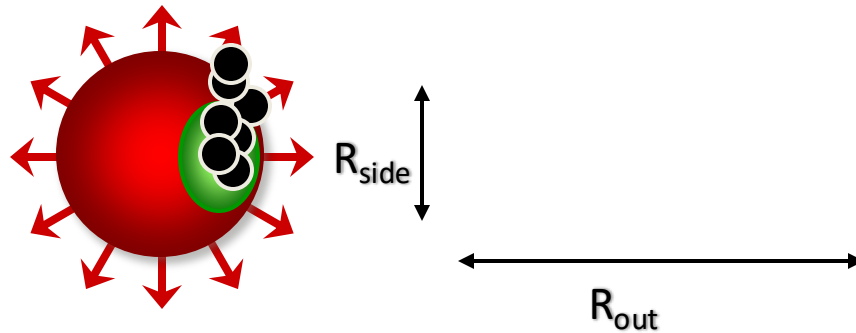
● kaon

3D info and timescale

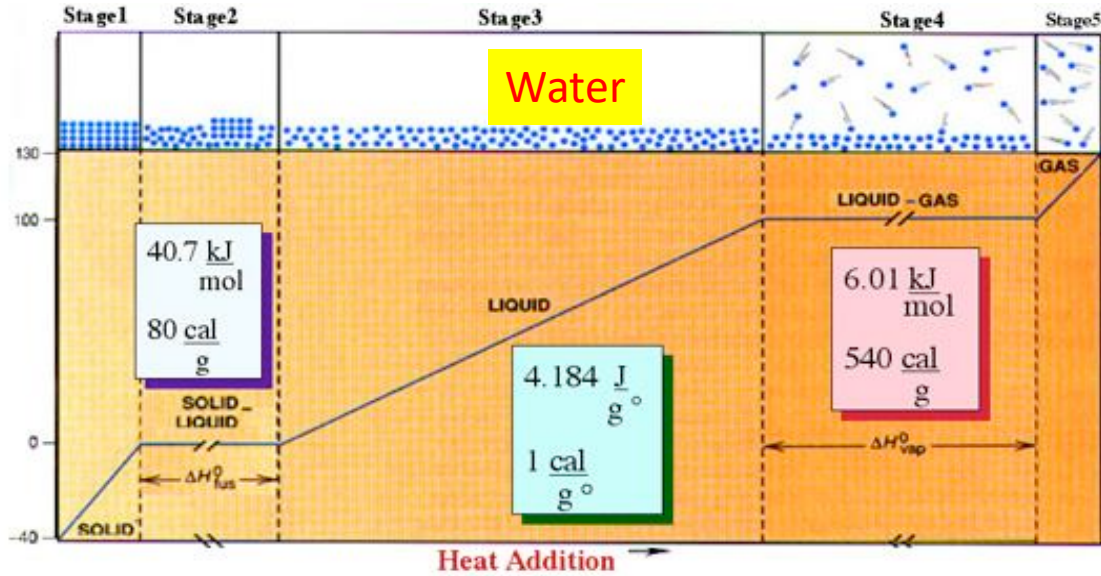
Bertsch-Pratt decomposition: R_{out} , R_{side} , R_{long}



A long emission duration results in $R_{out} > R_{side}$



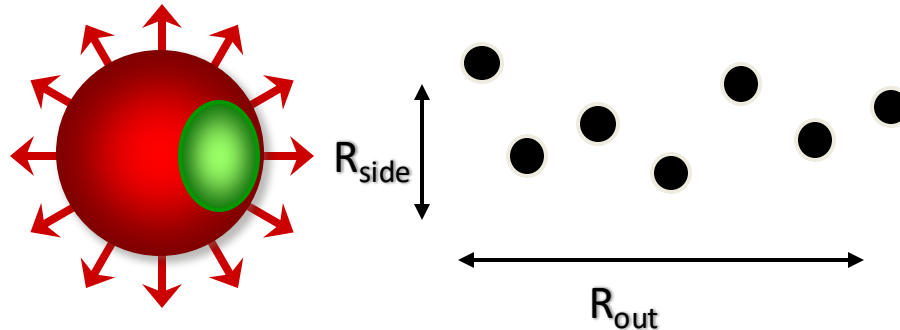
Phase transition? Order?



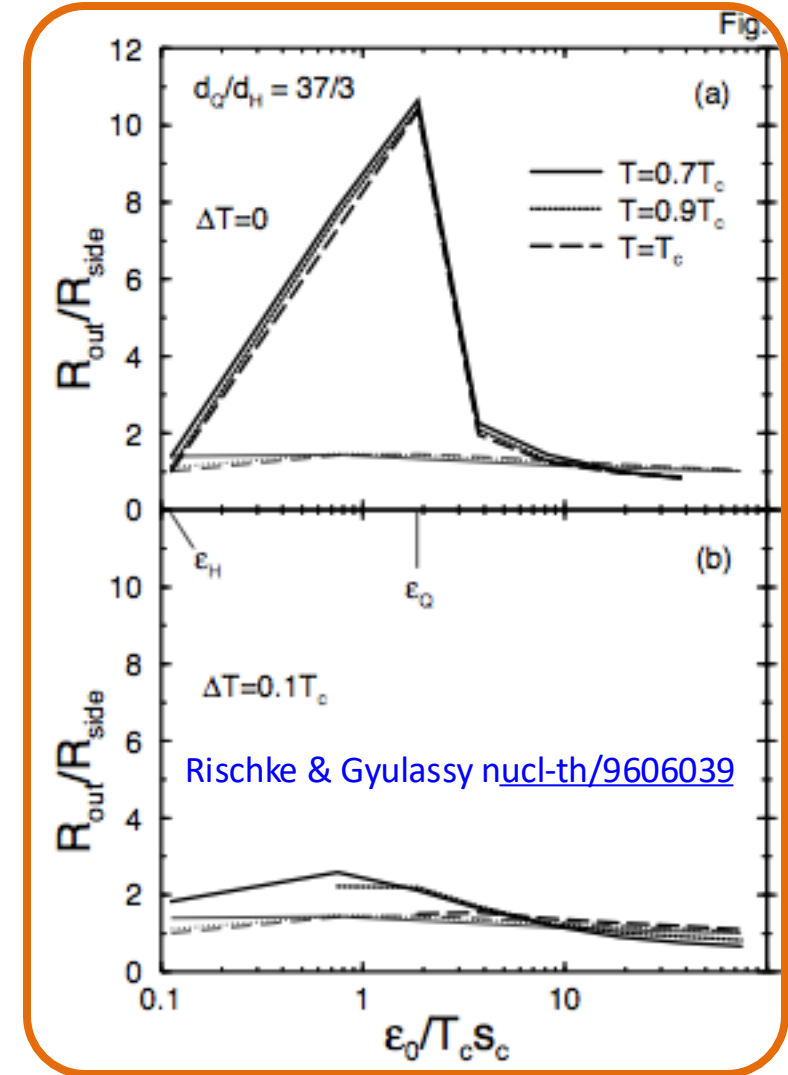
Probe for phase transition → vary conditions

RHIC Beam Energy Scan

A long emission duration results in $R_{out} > R_{side}$

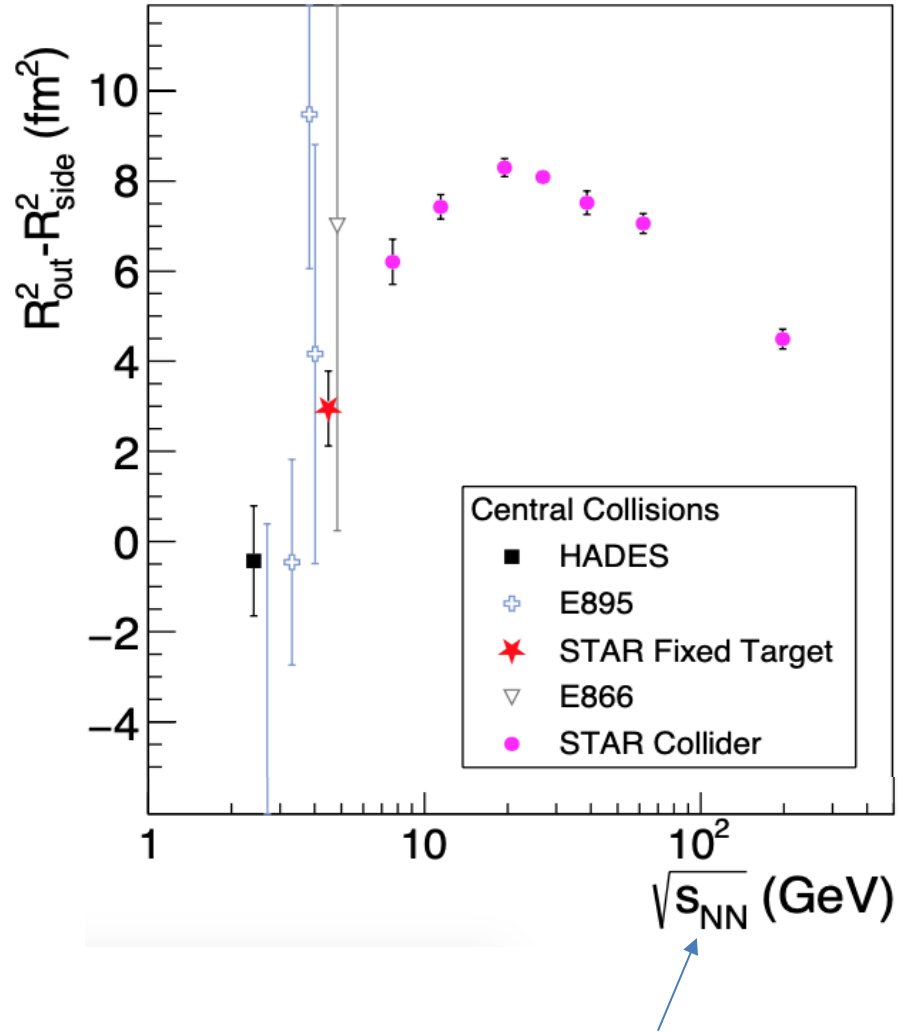


Early expectations at RHIC 200 GeV



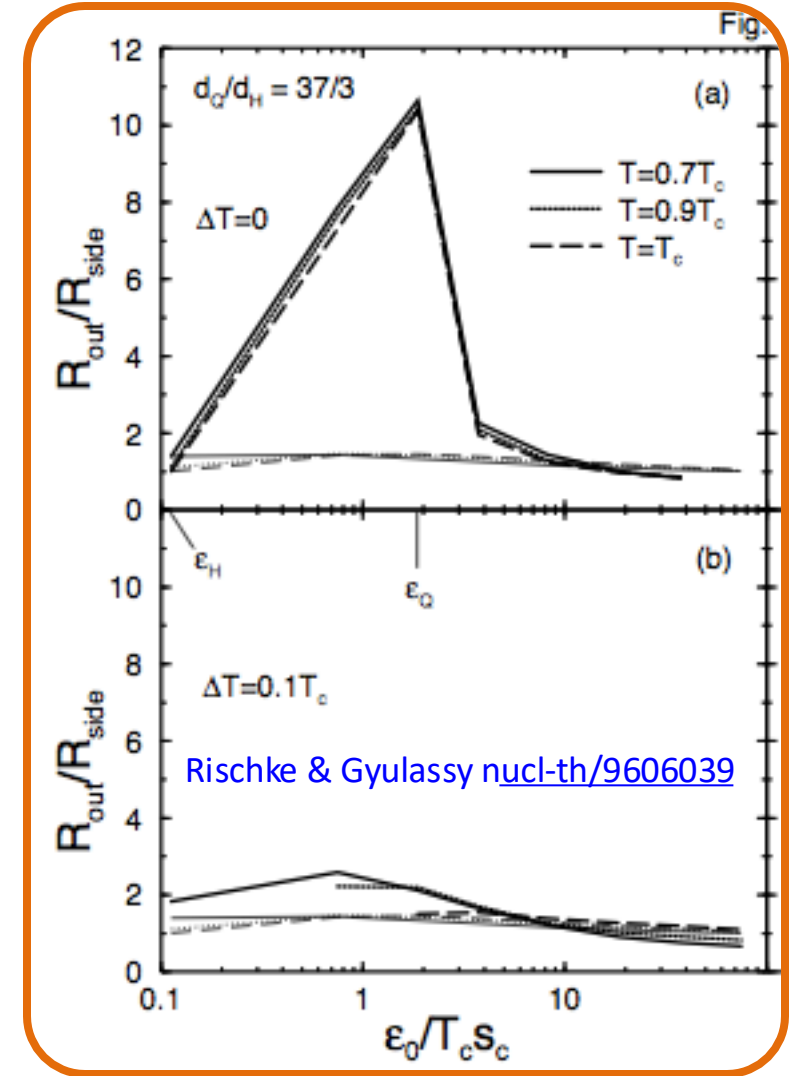
Phase transition? Order?

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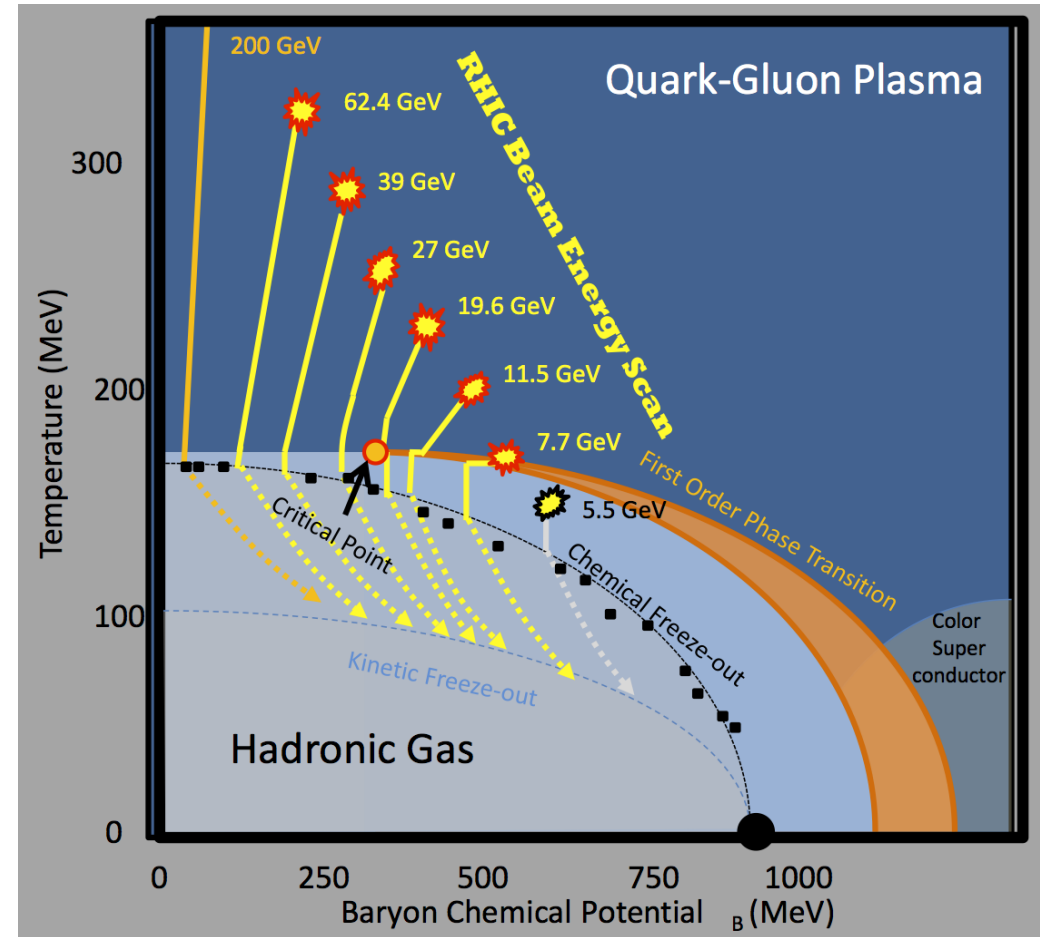
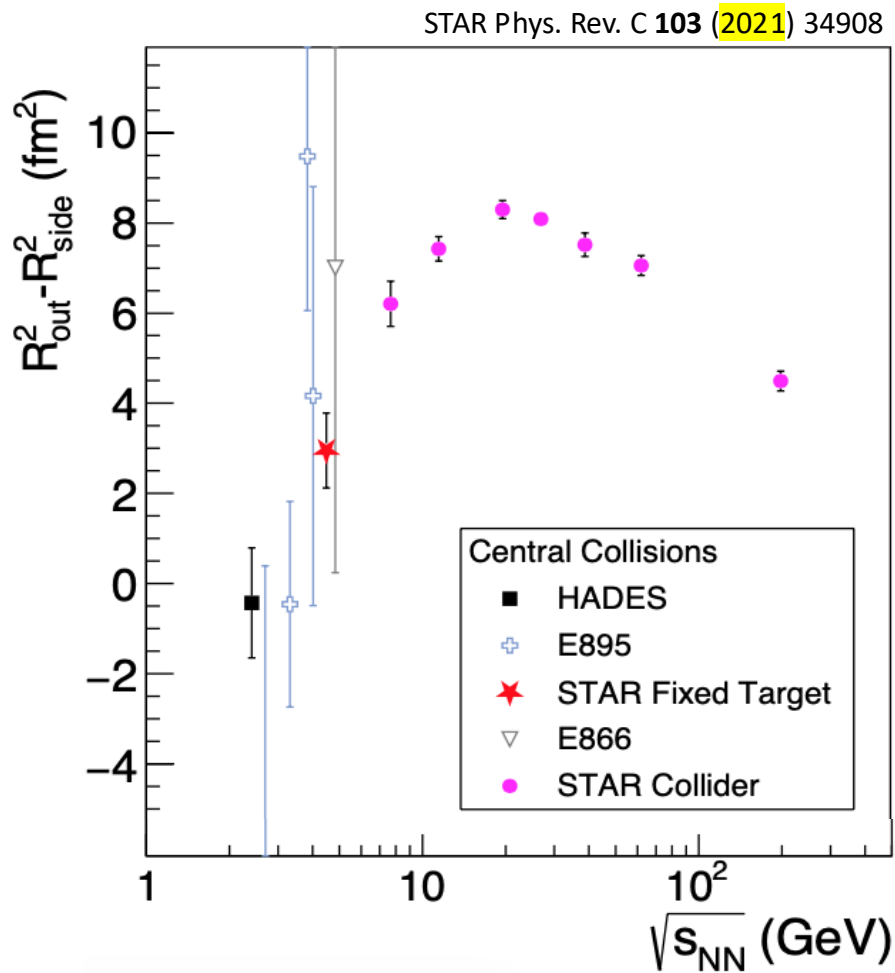


Multi-year program (BES) to vary the collision energy

Early expectations at RHIC 200 GeV



Phase transition? Order?



Evidence for

- cross-over at high energy (low chemical potential)
- first-order phase transition ~ 15 GeV

Summary

- Subatomic intensity interferometry (femtoscscopy) deeply connected to HBT
 - Through Koonin-Pratt equation, sII has more probes than SII (“particle zoo” to correlate)
- Experimental access to spacetime features of relativistic heavy ion collisions is essential to understanding the quark-gluon plasma and QCD phase structure
- Active community of femtoscopists measuring
 - size, shape, orientation, emission duration, evolution time, flow substructure
- Cross-disciplinary discussion is interesting and can be fruitful!



Scales of SII and sII

SII – example: γ Cas	
$R \sim 10 R_{\odot} \sim 10^{10} \text{ m}$	$2R/d \sim 4 \times 10^{-9} \sim \text{milliarcsec}$
$d \sim 500 \text{ ly} \sim 5 \times 10^{18} \text{ m}$	
$b \sim 100 \text{ m}$	$\lambda/b \sim 4 \times 10^{-9} \sim \text{milliarcsec}$
$\lambda \sim 4 \times 10^{-7} \text{ m}$	
sII (femtoscscopy) – example Au+Au @ RHIC	
$R \sim 5 \text{ fm} \sim 5 \times 10^{-15} \text{ m}$	$2R/d \sim 10^{-14} \sim 2 \text{ nanoarcsec}$
$d \sim 1 \text{ m}$	
$b \sim 1 \text{ m}$	$\lambda/b \sim 5 \times 10^{-16} \sim 0.1 \text{ nanoarcsec}$
$\lambda \sim hc/(400 \text{ MeV}) \sim 5 \times 10^{-16} \text{ m}$	

